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 Meng, X.-L. (2018) Statistical Paradises and Paradoxes in Big Data (I): Law of Large Populations, Big Data Paradox, and The 2016 US Election. Annals of Applied Statistics Vol 2: 685-726

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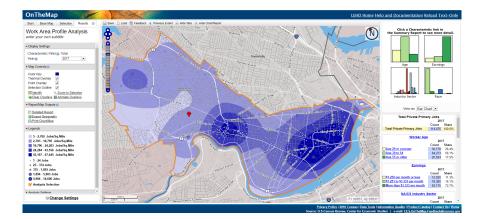
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- Thanks to many students and colleagues for augmenting my intelligence, and to on-line sources for enhancing my presentation.

#### OnTheMap Project of US Census Bureau



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  - Unemployment Insurance record was never intended for statistical inference purposes.

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- But is an 80% non-random sample "better" than a 5% random sample in measurable terms? 90%? 95%? 99%? (Jeremy Wu 2012)
- "Which one should we trust more: a 1% survey with 60% response rate or a non-probabilistic dataset covering 80% of the population?" (Keiding and Louis, 2016, Journal of Royal Statistical Society, Series B)

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- Landmark paper: Neyman (1934)
- First implementation in 1940 US Census led by Morris Hansen



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• Think about tasting soup

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- Think about tasting soup
- Stir it well, then a few bits are sufficient regardless of the size of the container!





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• But what happens when we fail to stir (well)?

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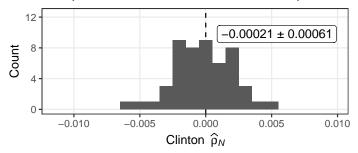
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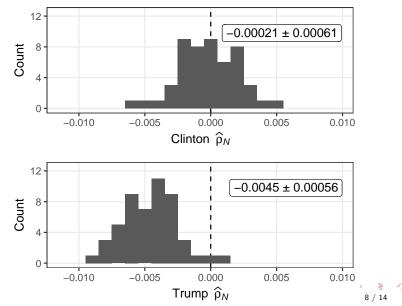
Three and only three ways to control the estimation error:

$$\underbrace{\bar{X}_n - \bar{X}_N}_{\text{Estimation Error}} = \underbrace{\operatorname{Corr}(R, X)}_{\text{Data Quality}} \times \underbrace{\sqrt{\frac{N-n}{n}}}_{\text{Data Quantity}} \times \underbrace{\operatorname{St.Dev}(X)}_{\text{Problem Difficulty}}.$$

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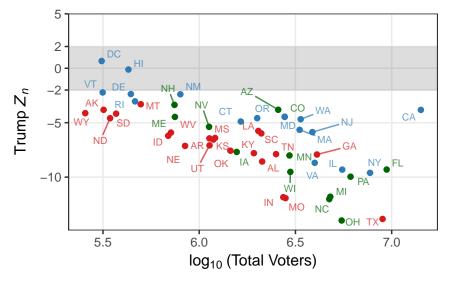
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• Butterfly Effect due to Law of Large Populations (LLP)

Relative Error =  $\sqrt{N-1}\hat{\rho}_{N}$ 

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LLP: The more voters, the higher the bias in our prediction



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#### The Big Data Paradox:

If we do not pay attention to data quality, then

# The bigger the data, the surer we fool ourselves.

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#### Three Enemies of Surveys and Data Science in General

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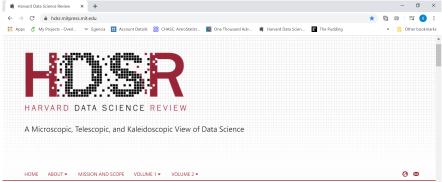
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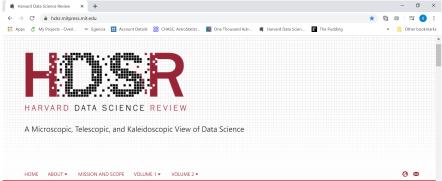
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#### More Lessons From ...



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#### PANORAMA

Overviews, Visions, and Debates

#### Teresa A. Sullivan

Coming To Our Census: How Social Statistics Underpin Our Democracy (And Republic)

Commentary by: Margo J. Anderson - Thomas R. Belin - Ray Chambers - Constance F. Citro - Reynolds Farley - Howard Hogan - Karen Kafadar - Dudley L. Poston, Jr. -Dennis Trewin

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Differential Privacy and Social Science: An Urgent Puzzle

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