

Population Estimation

United Nations Statistics Division



Outline

- 1. The Population Balancing Equation
- 2. Intercensal Cohort Survival Rates
- 3. Cohort Component Method



Population Balancing Equation

Census coverage



If a country has:

- A relatively complete system of vital registration
- A fairly reliable estimate of the degree of under-registration
- Information on the number of intercensal births, deaths and net international migrants can be used in conjunction with the results of a previous census to evaluate the coverage of a subsequent or current census.



$P_1 = P_0 + (B - D) + (I - E)$

Where:

- P_1 = Population enumerated in the census being evaluated
- P_0 = Population enumerated in a previous census
- B = Number of births in the period between the two censuses
- D= Number of deaths in the period between two censuses
- I = Number of international immigrants during the intercensal period
- E = Number of international emigrants during the intercensal period



- The population balancing equation is the most fundamental equation in demographic analysis and is also used to estimate population growth.
- □ It is based on the logic that:

The population of a country can increase or decrease between any two points in time **only** as a result of births, deaths and movement of population across national boundaries

- > Births and immigration contribute to increase the population
- > Deaths and emigration reduce the population



- For census evaluation purposes, there is a residual (e) needed to make the equation balance exactly
- "e" in the equation is referred to as the "error of closure" and represents the balance of errors in the data on births, deaths, net migration, and the coverage of the two censuses:

$$P_1 = P_0 + (B - D) + (I - E) + e$$

If e < 0 (negative), P₁ is under-enumerated relative to P₀
If e > 0 (positive), P₁ is over-enumerated relative to P₀



Population balancing equation – Data required

- The population enumerated in two consecutive censuses
 - > P_1 : Census under evaluation
 - > P_0 : Previous census
- The number of births, deaths and net international migration (immigrants – emigrants) during the intercensal period, adjusted for under-registration (to the extent possible)



Population balancing equation – Computational Procedure

1. Compile registered numbers of intercensal births, deaths and migrants

- Vital registration system
- Immigration record system (residence permit, border records, etc.)
- Adjustment based on under-coverage of these systems including indirect estimates
- **2.** Calculation of the "expected" census population (E(P1))

E(P1) = P0 + (B - D) + (I - E)

3. Calculation of the residual error or error of closure

 $e = P_1 - E(P_1)$



Population balancing equation – Interpretation of "e"

- If P₀ has been adjusted for net coverage error, the estimated residual error (e) will represent an estimate of net coverage error in P₁
 - > If "e" is positive, P_1 is over-enumerated
 - > If "e" is negative, P₁ is under-enumerated
- If P₀ is not adjusted, "e" will represent an estimate of the relative level of net coverage error in P₁ in comparison with P₀



Population balancing equation – Example Sri Lanka, 1971 and 1981 Censuses (1)

For an unadjusted census:

- $E(P_1) = P_0(unadjusted) + B_{adj} D_{adj} + M_{adj}$
 - = 12,689,897 + 3,716,878 1,002,108 + (-446,911)
 - = 14,957,756
- $e = P_1 E(P_1)$
 - = 14,848,364 14,957,756
 - $= -109,392 \ 0.7\% \ of E(P_1)$

>> P₁ is under-enumerated relative to P₀

Source: U.S. Census Bureau (1985)



Population balancing equation – Example Sri Lanka, 1971 and 1981 Censuses (2)

For an adjusted census count:

- $E(P_1) = PO(adjusted) + B_{adj} D_{adj} + M_{adj}$
 - = **12,849,796** + 3,716,878 1,002,108 + (-446,911)

= 15,117,655

- $e = P_1 E(P_1)$
 - = 14,848,364 15,117,655
 - $= -269,291 \ 1.8\% \ of E(P_1)$

>> P₁ is under-enumerated relative to P₀

Source: U.S. Census Bureau (1985)



Population balancing equation – Limitations

- Incomplete and defective data on the components of population change are very common
 - Applicability of the method is limited to countries with good vital registration coverage and migration data
- It is generally not useful for obtaining estimates of net census coverage error for sub-national populations (for example regions, provinces).
 - In addition to the components of population change considered, internal migration has to be considered
 - For most practical purposes, the use of the population balancing equation is limited to analysis of net coverage error at the national level



Cohort Survival Ratios

Mortality and census coverage

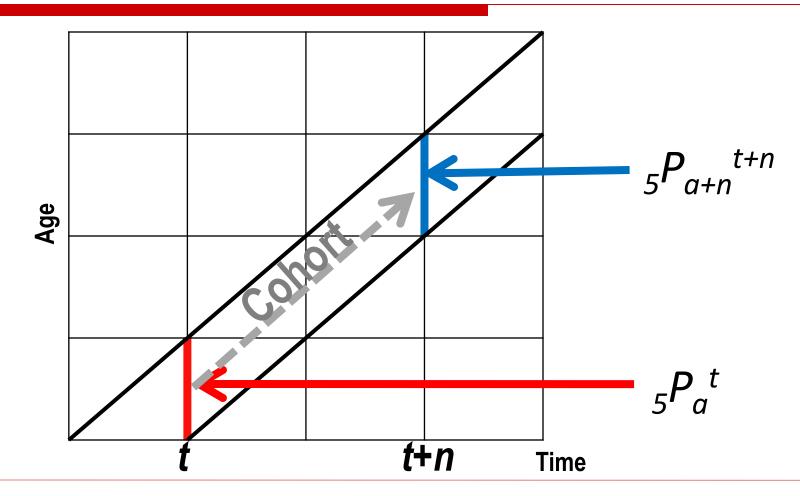


(Intercensal) Cohort survival ratios (CSR)

- This technique is based on a comparison of the size of birth cohorts enumerated in successive censuses
- In the absence of census errors, the ratio of the number of persons in a cohort enumerated in the second census to the number enumerated in the first census should approximate the survival rate that would be expected on the basis of mortality conditions
 - E.g. we have a cohort of males aged 40-44 at the time of the first census, say in 2000
 - If the next census is held exactly 10 years later, in 2010, this cohort will be aged 50-54
 - In the absence of other factors, we expect their numbers to have been reduced only by the life table quantity ${}_{10}d_x = l_x l_{x+n}$, the number of deaths to those aged x over the subsequent 10 years



Cohort survival analysis: the principle



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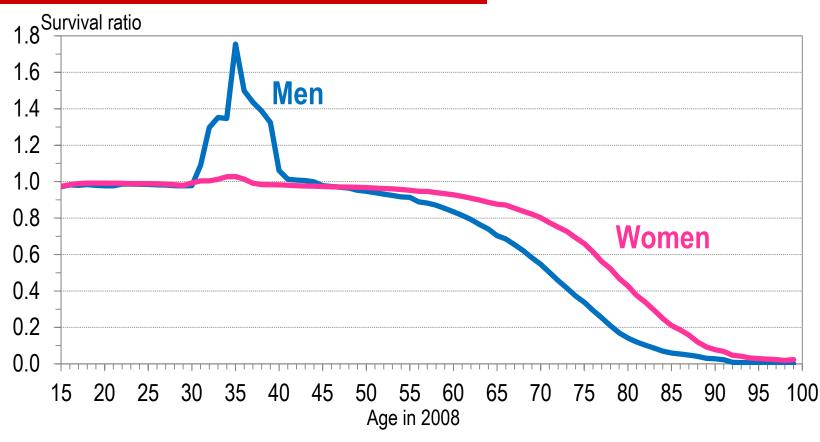


Cohort Survival Ratios: Caveats

- The method is less useful when other factors make it difficult to determine whether deviations from the expected CSR are due to census error or something else
 - Substantial net migration (unless there are accurate estimates of net migration by age)
 - Changes in country borders between censuses
 - Changes in the population groups included in the two censuses (e.g. active military, nomadic groups) if the size of these groups is substantial



Cohort Survival Ratios: DPR Korea (1993-2008)

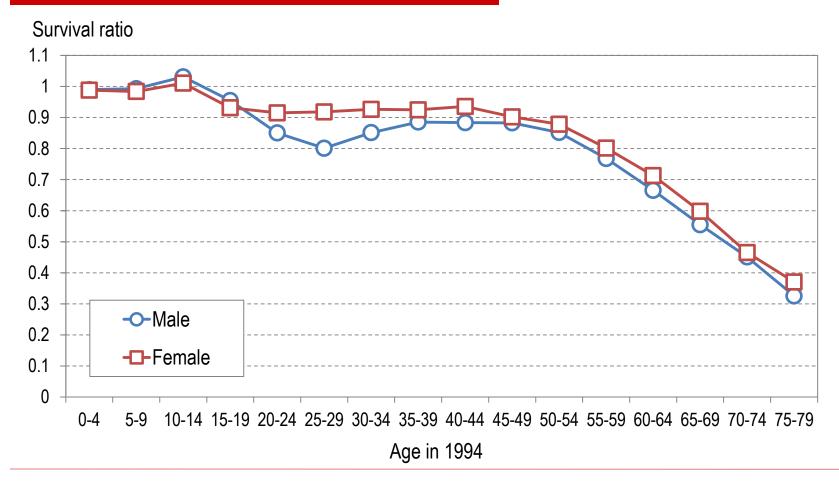


Source: Spoorenberg & Schwekendiek (2012).

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Cohort Survival Ratios: Jordan, 1994 & 2004 Censuses



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Calculating CSR(1)

Intercensal cohort survival rates are defined as:

$${}_{n}CSR_{x}(a) = \frac{{}_{n}P_{x+a}(t+a)}{{}_{n}P_{x}(t)}$$

Where:

- *t* = time of first census
- *a* = number of years between censuses
- ${}_{n}P_{x}(t)$ = size of the cohort at the time of the first census
- ${}_{n}P_{x+a}(t+a)$ = size of the cohort at the time of the second census



Calculating CSR (2)

The ratio of the observed intercensal cohort survival rate to the corresponding life-table survival rate

$${}_{n}R_{x} = \frac{\frac{{}_{n}P_{x+a}(t+a)}{{}_{n}P_{x}(t)}}{\frac{{}_{n}L_{x+a}}{{}_{n}L_{x}}}$$

Where:

- $_{n}P_{x+a}(t+a)$ = size of the cohort at time of the second census
- $_{n}P_{x}(t)$ = size of the cohort at the time of the first census
- ${}_{n}L_{x+a}$ = life table number of person-years lived in age interval x+a to x+a+n years
- $_{n}L_{x}$ = life table number of person-years lived in age interval x to x+n years



Cohort Survival Ratio - Interpretation

In the **absence of census error**, the expected value of the ratio $\binom{n}{n}R_x$ would be **1.0**

Ratio values for any particular cohort which **exceed 1.0** would indicate **over-enumeration** of the cohort in the second census relative to the first census

Ratio values of **less than 1.0** would indicate **under-enumeration** of the cohort in the second census relative the first census



Cohort Survival Ratio – Possible bias

Discrepancies can be due to 3 factors:

- Actual census errors
- Deficient data/adjustments for migration
- Wrong life table



Cohort survival ratios – Example (1)

Step 1: Adjustment for migration (*if appropriate*)

- In countries experiencing significant levels of net intercensal immigration, the number of net immigrants in each cohort may either added to the cohort enumerated in the first census or subtracted from the cohort enumerated in the second census
- In cohorts experiencing net intercensal emigration, the number of net intercensal emigrants can either added to the second census or subtracted from the first census
- Should be confident that migration data is reasonably accurate before making any adjustments



Cohort survival ratios – Example (2)

Step 2: Calculation of census survival rates using two consecutive censuses $>_{n}P_{x+a}(t+a)/_{n}P_{x}(t)$

| 1 Aug 2000 | | | 1 Aug 2010 | | | Cohort Survival Ratio 2000 - 2010 | | |
|------------|-----------|-----------|------------|-----------|-----------|-----------------------------------|--------|--|
| Age | Male | Female | Age | Male | Female | Male | Female | |
| 0 - 4 | 8,326,926 | 8,048,802 | 0 - 4 | | | | | |
| 5 - 9 | 8,402,353 | 8,139,974 | 5 - 9 | | | | | |
| 10-14 | 8,777,639 | 8,570,428 | 10.14 | 8,725,413 | 8,441,348 | 1.0479 | 1.0488 | |
| 15 - 19 | 9,019,130 | 8,920,685 | 15 - 19 | 8,558,868 | 8,432,002 | 1.0186 | 1.0359 | |
| 20 - 24 | 8,048,218 | 8,093,297 | 20 - 24 | 8,630,227 | 8,614,963 | 0.9832 | 1.0052 | |
| 25 - 29 | 6,814,328 | 7,035,337 | 25 - 29 | 8,460,995 | 8,643,418 | 0.9381 | 0.9689 | |
| 30 - 34 | 6,363,983 | 6,664,961 | 30 - 34 | 7,717,657 | 8,026,855 | 0.9589 | 0.9918 | |
| 35 - 39 | 5,955,875 | 6,305,654 | 35 - 39 | 6,766,665 | 7,121,916 | 0.9930 | 1.0123 | |
| 40 - 44 | 5,116,439 | 5,430,255 | 40 - 44 | 6,320,570 | 6,688,797 | 0.9932 | 1.0036 | |
| 45 - 49 | 4,216,418 | 4,505,123 | 45 - 49 | 5,692,013 | 6,141,338 | 0.9557 | 0.9739 | |
| | | | | | | | | |



Cohort survival ratios – Example (3)

Step 3: Calculation of life table survival rates based on the expected level of mortality $_{n}S_{x} = \frac{nL_{x+a}}{nL_{x}}$

For first age group (here age 5-9): ${}_{n}S_{x} = \frac{nL_{x+a}}{L_{0} + L_{1}}$

For open-ended age group:

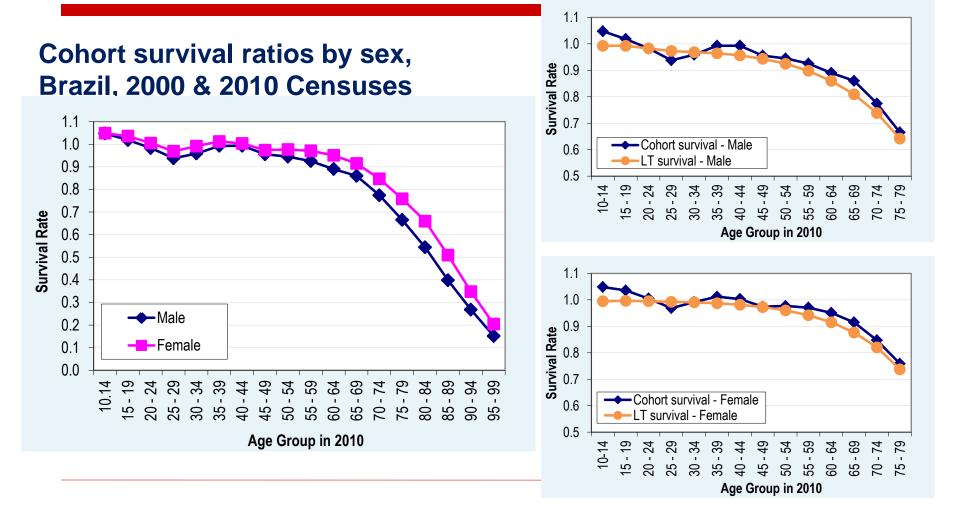
$${}_{w}S_{x} = \frac{{}_{w}T_{x+a}}{{}_{n}T_{x}}$$

Step 4: Calculation of cohort survival ratios (*nRx*)

| 1 Aug 2000 | | 1 Aug 2010 | | | Cohort Survival Ratio 2000 - 2010 | | Life Table Survival Rate | | nRx | | |
|----------------|-----------|------------|----------------|-----------|--------------------------------------|--------|-----------------------------|--------|--------|--------|--------|
| | Male | Female | | Male | Female | Male | Female | Male | Female | Male | Female |
| 0 - 4 | 8'326'926 | 8'048'802 | 0 - 4 | | | | | | | | |
| 5 - 9 | 8'402'353 | 8'139'974 | 5 - 9 | | | | | | | | |
| 10-14 | 8'777'639 | 8'570'428 | 10.14 | 8'725'413 | 8'441'348 | 1.0479 | 1.0488 | 0.9928 | 0.9950 | 1.0554 | 1.0541 |
| 15 - 19 | 9'019'130 | 8'920'685 | 15 - 19 | 8'558'868 | 8'432'002 | 1.0186 | 1.0359 | 0.9928 | 0.9966 | 1.0261 | 1.0394 |
| 20 - 24 | 8'048'218 | 8'093'297 | 20 - 24 | 8'630'227 | 8'614'963 | 0.9832 | 1.0052 | 0.9830 | 0.9951 | 1.0002 | 1.0102 |
| 25 - 29 | 6'814'328 | 7'035'337 | 25 - 29 | 8'460'995 | 8'643'418 | 0.9381 | 0.9689 | 0.9733 | 0.9930 | 0.9639 | 0.9758 |
| 30 - 34 | 6'363'983 | 6'664'961 | 30 - 34 | 7'717'657 | 8'026'855 | 0.9589 | 0.9918 | 0.9685 | 0.9907 | 0.9901 | 1.0011 |
| 35 - 39 | 5'955'875 | 6'305'654 | 35 - 39 | 6'766'665 | 7'121'916 | 0.9930 | 1.0123 | 0.9643 | 0.9873 | 1.0298 | 1.0253 |
| 40 - 44 | 5'116'439 | 5'430'255 | 40 - 44 | 6'320'570 | 6'688'797 | 0.9932 | 1.0036 | 0.9566 | 0.9818 | 1.0383 | 1.0222 |
| 45 - 49 | 4'216'418 | 4'505'123 | 45 - 49 | 5'692'013 | 6'141'338 | 0.9557 | 0.9739 | 0.9436 | 0.9729 | 1.0128 | 1.0010 |



Cohort survival ratios – Example (4)





Cohort Survival: Uses and limitations

- It is a widely applicable approach for examining error in consecutive censuses
- Method requires relatively little information
 - Information on the level of fertility is not required since the method does not assess the coverage of the population born between two censuses
- Method is complicated by migration etc. as discussed
- When only two censuses are available, the method suffers from the limitations shared by many demographic methods, namely difficulties in separating census errors from real irregularities caused by extraordinary events
 - The utility of census survival approaches increases significantly when three or more censuses are available

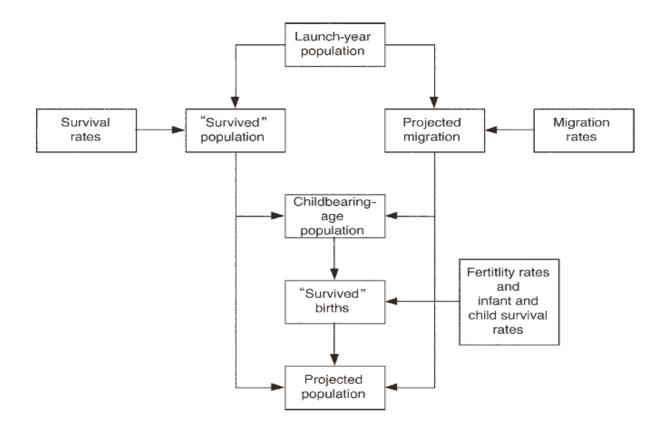


Cohort Component Method

Population estimation



Overview of cohort-component method



Smith, S., J. Tayman, and D. A. Swanson. 2001. State and Local Population Projections: Methodology and Analysis. New York: Kluwer Academic/Plenum Publishers.

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Cohort component method (CCM)

- In this approach, the population enumerated in the first census is projected to the reference date of the second census based on estimated levels and age schedules of fertility, mortality and migration during the intercensal period
- The expected population from the projection is then compared with the actual population enumerated in the second census
- Data for intercensal births, deaths and migration are taken from estimates and/or assumptions regarding the level and age schedules of these parameters rather than directly available data based on registration systems



Cohort component method (CCM) – data required

- 1. Population enumerated in two censuses by age and sex
- Age specific fertility rates for women aged 15 to 49 (in 5-year age groups), assumed to represent the level and age structure of fertility during the intercensal period
- 3. Life table survival rates for males and females, assumed to be representative of mortality conditions during the intercensal period
- 4. An estimate of sex ratio at birth
- Estimates of the level and age pattern of net international migration during the intercensal period if the level of net migration is substantial



CCM– overview of computational steps

- 1. "Survive" the age distribution at the initial census to the time of the second census
 - a) Multiply each age group population by life table survival rates
 - b) Open-ended interval requires special handling
- 2. Calculate the total number of births (total, by sex) during the period
- 3. Make any necessary adjustments for migration
 - a) Average initial and projected population for each age group between 15-49 to estimate mid-period female population
 - b) Apply age-specific birth rates to these populations to generate total numbers of births during time period
 - c) Apply sex ratio factor to get female and male births from total births
- 4. Apply life table survivorship to these births to determine number that survive to time of the second census
- 5. Compare the estimated population by age group with the enumerated population at the second census



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CCM – Step 1 (survive initial age distribution)

Still need to estimate youngest cohorts based on fertility data

"Survive" the age distribution at the initial census to the time of the second census

$${}_{n}S_{x} = \frac{{}_{n}L_{x+a}}{{}_{n}L_{x}}$$

First age group (age 5-9):

$${}_nS_x = \frac{{}_nL_{x+a}}{{}_1L_0 + {}_4L_1}$$

Open-ended age group:

$${}_{w}S_{x} = \frac{{}_{w}T_{x+a}}{{}_{n}T_{x}}$$

with a = time between census

| al | Age | Total population, 2000 Census | | Life ta survival | | Projected population, 2005 | | |
|----|-------|----------------------------------|---------|-------------------------------|-------------------------------|-------------------------------|---------------|--|
| | | Male | Female | 5 ^L x ^M | ₅ L _x F | Male | Female | |
| | 0-4 | 124,482 | 121,541 | • | • | | | |
| | 5-9 | 144,315 | 141,349 | 0.99201 | 0.99393 | 123,487 | 120,804 | |
| | 10-14 | 159,294 | 158,140 | 0.99746 | 0.99838 | 143,949 | 141,121 | |
| | 15-19 | 133,327 | 130,031 | 0.99659 | 0.99819 | 158,750 | 157,855 | |
| | 20-24 | 118,023 | 117,728 | 0.99302 | 0.99669 | 132,396 | 129,601 | |
| | 25-29 | 107,962 | 108,690 | 0.98837 | 0.99491 | 116,650 | 117,129 | |
| | 30-34 | 92,473 | 95,399 | 0.98261 | 0.99263 | 106,084 | 107,889 | |
| | 35-39 | 84,846 | 87,760 | 0.97579 | 0.98965 | 90,234 | 94,411 | |
| | 40-44 | 62,619 | 64,601 | 0.96477 | 0.98415 | 81,856 | 86,369 | |
| | 45-49 | 40,562 | 42,326 | 0.94594 | 0.97379 | 59,234 | 62,908 | |
| | 50-54 | 27,707 | 30,128 | 0.92103 | 0.95724 | 37,359 | 40,516 | |
| | 55-59 | 27,379 | 28,516 | 0.89899 | 0.93869 | 24,908 | 28,281 | |
| | 60-64 | 20,778 | 21,514 | 0.85823 | 0.91338 | 23,497 | 26,046 | |
| | 65-69 | 15,982 | 19,433 | 0.79296 | 0.87437 | 16,476 | 18,811 | |
| | 70+ | 18,232 | 28,356 | 0.58241 | 0.64549 | 19,927 | 12,544 | |



CCM – Step 2 (adjust for migration *if needed*)

If net international migration is substantial, the "survived" cohort population must be adjusted to reflect the effects of migration

The introduction of net migrants by age group at the mid-point of the projection period and the survival of net migrants to the end of the period:

$$_{n}\hat{M}_{x+i} = \frac{1}{4} {}_{n}M_{x}(1+{}_{n}S_{x}) + \frac{1}{4} {}_{n}M_{x+i}(1+{}_{n}S_{x+i})$$

Assumptions:

- i) An equal distribution of net migrants across years of the intercensal period,
- ii) Migrants have the same fertility and mortality level as the enumerated population



CCM – Step 3 (Calculate births)

 Calculate the average number of women in each childbearing age group (15-49) during the intercensal period in order to estimate the number of births during the projection period

$$_{n}\overline{P}_{x} = \frac{_{n}P^{0}{}_{x} + _{n}P^{t}{}_{x}}{2}$$

 $_{n}\overline{P}_{x}$ = average number of females aged *x* to *x*+*n* in the projection period $_{n}P_{x}^{0}$ = number of females aged *x* to *x*+*n* at the beginning of the projection period $_{n}P_{x}^{t}$ = projected number of females aged *x* to *x*+*n* at the end of the projection period



CCM – Step 3 (Calculate births)

2. Calculate total births during the period, for 5-year projections:

$$B = 5 \cdot \sum_{x=15} \left({}_{n} \bar{P}_{x} \cdot {}_{n} f_{x} \right)$$

Where

B = estimated number of births in the projection period

 $_{n}\overline{P}_{x}$ = average number of females aged x to x+n in the projection period

 f_x = Age-specific fertility rate for women age x to x+n years during the projection period

| | Female population, 2000 census | Female population, 2005 projected | Female population, mid-period | ASFR, ₅F _x | Number of births, B | |
|------------|--------------------------------|--------------------------------------|----------------------------------|-----------------------|------------------------|--|
| | (a) | (b) | (c) = ((a)+(b))/2 | (d) | $(e) = (c)^{*}(d)$ | |
| 15-19 | 130,031 | 157,855 | 143,943 | 0.02155 | 3,102 | |
| 20-24 | 117,728 | 129,601 | 123,664 | 0.12858 | 15,901 | |
| 25-29 | 108,690 | 117,129 | 112,909 | 0.12671 | 14,307 | |
| 30-34 | 95,399 | 107,889 | 101,644 | 0.08179 | 8,314 | |
| 35-39 | 87,760 | 94,411 | 91,086 | 0.04031 | 3,672 | |
| 40-44 | 64,601 | 86,369 | 75,485 | 0.01262 | 953 | |
| 45-49 | 42,326 | 62,908 | 52,617 | 0.00357 | 188 | |
| TFR | | | | 2.08 | | |
| Total 5*∑e | | | | | 232,183 | |



CCM – Step 3 (calculate M/F births)

3. Calculate proportion of male and female births

For female births:

$$B^{f} = \left(1 - \frac{\text{sex ratio at birth}}{1 + \text{sex ratio at birth}}\right) \cdot B$$
$$B^{f} = \left(1 - \frac{1.05}{1 + 1.05}\right) \cdot B = 0.488 \cdot B \quad \Rightarrow B^{f} = 0.488 \cdot 232,183$$
$$B^{f} = 113,305$$

For male births:

$$B^{m} = \left(\frac{\text{sex ratio at birth}}{1 + \text{sex ratio at birth}}\right) \cdot B$$
$$B^{m} = \left(\frac{1.05}{1 + 1.05}\right) \cdot B = 0.512 \cdot B \qquad \rightarrow B^{m} = 0.512 \cdot 232,183$$
$$B^{m} = 118.877$$



CCM – Step 4 (Survive intercensal births)

4. Apply life table survivorship to these births to determine number that survive to time of the second census

For girls: ${}_{5}P_{0}^{f} = B^{f} \cdot {}_{5}S_{0}^{f}$ with ${}_{5}S_{0}^{f} = \frac{{}_{5}L_{0}^{f}}{5 * l_{0}}$ ${}_{5}S_{0}^{f} = 480,143/500,000 = 0.96029$ $\rightarrow {}_{5}P_{0}^{f} = 113,305 \cdot 0.96029 = 108,805$

For boys:

 ${}_{5}P_{0}^{m} = B^{m} \cdot {}_{5}S_{0}^{m}$ with ${}_{5}S_{0}^{m} = \frac{{}_{5}L_{0}^{m}}{5 * l_{0}}$

 $_{5}$ S^m₀ = 476,147/500,000 = 0.95229

 $\rightarrow {}_{5}P^{f}_{0} = 118,877 \cdot 0.95229 = 113,206$



Mongolia, projection of the 2000 census population

| Age | Total population, 2000 Census | | Life tab survival | | Projected population, 2005 | |
|-------|----------------------------------|-------------|---------------------------|----------|-------------------------------|---------|
| | Male | Female | 5 L x ^M | 5LxF | Male | Female |
| 0-4 | 124,482 | 121,541 | 0.95229 | 0.96029 | 113,206 | 108,805 |
| 5-9 | 144,315 | 141,349 | 0.99201 | 0.99393 | 123,487 | 120,804 |
| 10-14 | 159,294 | 158,140 | 0.99746 | 0.99838 | 143,949 | 141,121 |
| 15-19 | 400.007 | 420.024 | 0.00050 | 0.00040 | 450 750 | 157,855 |
| 20-24 | | | | | | 129,601 |
| 25-29 | Procedure | is ronast | ed until the | next con | sus in 2010 | 117,129 |
| 30-34 | FIUCEUUI | = 15 Tepear | | | 5u5 III 2010 | 107,889 |
| 35-39 | | | | | | 94,411 |
| 40-44 | 62,619 | 64,601 | 0.96477 | 0.98415 | 81,830 | 86,369 |
| 45-49 | 40,562 | 42,326 | 0.94594 | 0.97379 | 59,234 | 62,908 |
| 50-54 | 27,707 | 30,128 | 0.92103 | 0.95724 | 37,359 | 40,516 |
| 55-59 | 27,379 | 28,516 | 0.89899 | 0.93869 | 24,908 | 28,281 |
| 60-64 | 20,778 | 21,514 | 0.85823 | 0.91338 | 23,497 | 26,046 |
| 65-69 | 15,982 | 19,433 | 0.79296 | 0.87437 | 16,476 | 18,811 |
| 70+ | 18,232 | 28,356 | 0.58241 | 0.64549 | 19,927 | 12,544 |

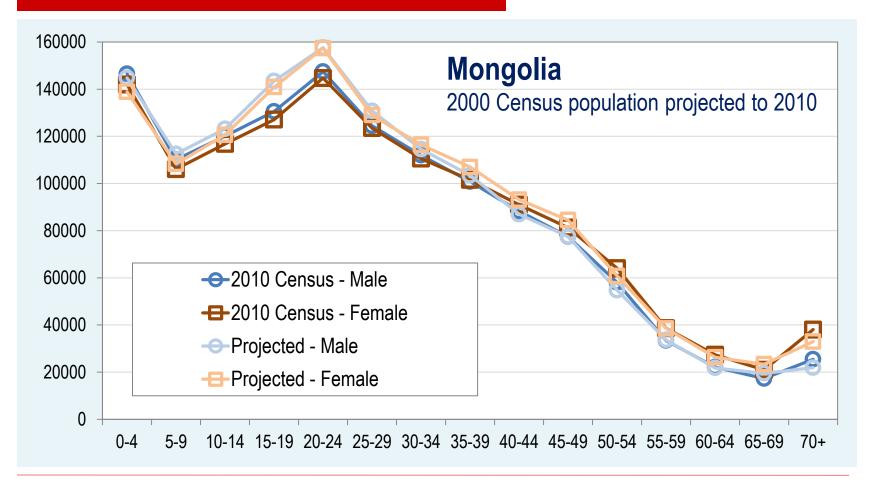


CCM – Step 5 (compare with enumerated population)

| | Projected population, 2005 | | Life table survival ratio | | Projected population, 2010 | | 2010 Census | |
|-------|-------------------------------|---------|------------------------------|-------------------------------|----------------------------|---------|-------------|---------|
| | Male | Female | ₅ L ^M | ₅ L _x F | Male | Female | Male | Female |
| 0-4 | 113,206 | 108,805 | 0.96434 | 0.96995 | 144,818 | 138,833 | 146,516 | 141,981 |
| 5-9 | 123,487 | 120,804 | 0.99409 | 0.99529 | 112,537 | 108,293 | 110,117 | 106,097 |
| 10-14 | 143,949 | 141,121 | 0.99739 | 0.99845 | 123,165 | 120,617 | 120,064 | 116,801 |
| 15-19 | 158,750 | 157,855 | 0.99664 | 0.99822 | 143,465 | 140,870 | 130,560 | 127,085 |
| 20-24 | 132,396 | 129,601 | 0.99296 | 0.99705 | 157,633 | 157,390 | 147,472 | 144,711 |
| 25-29 | 116,650 | 117,129 | 0.98781 | 0.99544 | 130,782 | 129,010 | 124,490 | 123,493 |
| 30-34 | 106,084 | 107,889 | 0.98236 | 0.99382 | 114,592 | 116,404 | 111,976 | 110,546 |
| 35-39 | 90,234 | 94,411 | 0.97525 | 0.99153 | 103,459 | 106,975 | 100,819 | 101,564 |
| 40-44 | 81,856 | 86,369 | 0.96365 | 0.98640 | 86,954 | 93,128 | 88,273 | 90,994 |
| 45-49 | 59,234 | 62,908 | 0.94665 | 0.97800 | 77,489 | 84,469 | 77,475 | 81,281 |
| 50-54 | 37,359 | 40,516 | 0.92422 | 0.96612 | 54,745 | 60,777 | 58,009 | 64,073 |
| 55-59 | 24,908 | 28,281 | 0.90131 | 0.95089 | 33,672 | 38,526 | 33,384 | 38,605 |
| 60-64 | 23,497 | 26,046 | 0.87393 | 0.92990 | 21,768 | 26,298 | 22,106 | 27,347 |
| 65-69 | 16,476 | 18,811 | 0.82943 | 0.89626 | 19,490 | 23,344 | 17,262 | 20,970 |
| 70+ | 19,927 | 30,847 | 0.58241 | 0.64549 | 21,873 | 32,944 | 25,445 | 38,029 |



CCM – Step 5 (compare with enumerated population)





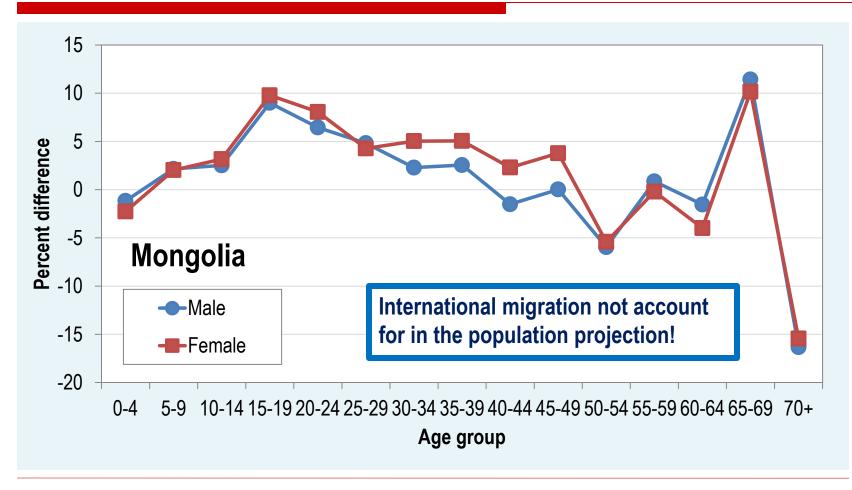
<u>CCM – Step 5 (compare with enumerated population)</u>

| | 2010 Projected population | | 2010 Enumerated population | | Absolute difference (Projected - Enumerated) | | Percent Difference (Abs. diff./Projected*100) | |
|------------|---------------------------|---------|----------------------------|---------|--|--------|--|--------|
| | Male | Female | Male | Female | Male | Female | Male | Female |
| 0-4 | 144818 | 138833 | 146516 | 141981 | -1698 | -3148 | -1.2 | -2.3 |
| 5-9 | 112537 | 108293 | 110117 | 106097 | 2420 | 2196 | 2.2 | 2.0 |
| 10-14 | 123165 | 120617 | 120064 | 116801 | 3101 | 3816 | 2.5 | 3.2 |
| 15-19 | 143465 | 140870 | 130560 | 127085 | 12905 | 13785 | 9.0 | 9.8 |
| 20-24 | 157633 | 157390 | 147472 | 144711 | 10161 | 12679 | 6.4 | 8.1 |
| 25-29 | 130782 | 129010 | 124490 | 123493 | 6292 | 5517 | 4.8 | 4.3 |
| 30-34 | 114592 | 116404 | 111976 | 110546 | 2616 | 5858 | 2.3 | 5.0 |
| 35-39 | 103459 | 106975 | 100819 | 101564 | 2640 | 5411 | 2.6 | 5.1 |
| 40-44 | 86954 | 93128 | 88273 | 90994 | -1319 | 2134 | -1.5 | 2.3 |
| 45-49 | 77489 | 84469 | 77475 | 81281 | 14 | 3188 | 0.0 | 3.8 |
| 50-54 | 54745 | 60777 | 58009 | 64073 | -3264 | -3296 | -6.0 | -5.4 |
| 55-59 | 33672 | 38526 | 33384 | 38605 | 288 | -79 | 0.9 | -0.2 |
| 60-64 | 21768 | 26298 | 22106 | 27347 | -338 | -1049 | -1.6 | -4.0 |
| 65-69 | 19490 | 23344 | 17262 | 20970 | 2228 | 2374 | 11.4 | 10.2 |
| 70+ | 21873 | 32944 | 25445 | 38029 | -3572 | -5085 | -16.3 | -15.4 |
| Total | 1346442 | 1377877 | 1313968 | 1333577 | 32474 | 44300 | 2.4 | 3.2 |
| Both sexes | 2724319 | | 2647545 | | 76774 | | 2.8 | |



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Percentage difference between expected (projected) and observed population, 2010 Census





Main findings from example of Mongolia

- Suggests overenumeration of more than 75 thousand people, or 2.8% of the population
- □ Slight underenumeration of youngest age group (age 0-4)
- Overenumeration starting from age 5-9 until 35-39 for males and 45-49 for females
 - Point to the fact that we did not account of international migration
 - Need to incorporate migration data
- Significant overenumeration of people age 65-69
 - Possibly related to age declaration
 - Possible also that life table used is not accurate for these ages



Cohort component method in MortPak (1)

- Computations made in Excel can be automated and done with more precision using the application PROJCT in MORTPAK
- PROJCT runs single-year population projection
- Data needed:
 - Population by age and sex,
 - Age patterns of mortality, fertility and migration,
 - Level of mortality, fertility and migration
- Results available by single years use drop-down menu to select year you want

>> Example of Mongolia using PROJCT



Cohort component method – uses and limitations

- It is applicable when registration data are not-existent or deficient to such an extent that satisfactory adjustment is not possible
- Sufficient information to derive estimates of fertility and mortality levels should be available
 - Mortality estimates can be complicated by HIV/AIDS with a generalized epidemic, one life table is generally not sufficient to model mortality patterns over a 10 year period
- Lack of information on international migration is often a problematic issue when applying this method
- In case where sufficient information exists to derive reliable estimates of demographic parameters, the method is perhaps the most powerful among the alternative demographic approaches for the evaluation of censuses, since it provides age and sex specific estimates of net census error







PROJCT application in MORTPAK – The United Nations software package for demographic measurement, available online: http://www.un.org/en/development/desa/population/publications/mortality/mortpak.shtml

DemProj module in Spectrum, available online at: <u>http://www.futuresinstitute.org/spectrum.aspx</u>

- DemProj is recommended for projection in contexts in which HIV/AIDS prevalence exceeds a few percent – better modeling of mortality conditions
- Requires more data input, including prevalence and treatment estimates for HIV/AIDS
- Data input options somewhat less flexible than MortPak



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To conclude...

"The problem of estimating demographic measures from incomplete data is a challenging one, one for which there is no universal answer and one which therefore requires in the demographer the qualities of resourcefulness and imagination."

(Pollard et al. 1990: 164)

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Thank you



Questions? >> until 12 December:



>> After 12 December: **spoorenberg@un.org**