

# **Evaluation of Child Mortality Data** from Population Censuses

**United Nations Statistics Division** 



#### **Outline**

#### 1. Life tables

- a) Constructing empirical (abridged) life tables
- b) Model life tables

#### 2. Survival of children ever born (Brass type estimates)

- a) Information required
- b) Checking data quality
- c) Estimation using MortPak (Qfive)
- d) Assumptions, violations, and assessing quality of estimates



## Life tables



#### Life tables

- One of demography's most influential discoveries
- Life table is useful to examine how many survive to successive ages and to determine the length of life
- Essential tool for population estimates and projections
- Important measure of progress
- Indicate whether the goal of long life for all is achieved
- Most widely known indicator >> Life expectancy at birth (e<sub>0</sub>)



## What is the life expectancy at birth $(e_0)$

#### Life expectancy at birth $(e_0)$

>> The expectation of life at exact age x, i.e. the average number of years lived by a person from exact age x

How to compute  $e_0$ ?



#### Crude Death Rate (CDR)

 $CDR[0, T] = \frac{\text{Number of deaths in the population between times 0 and } T}{\text{Number of person-years lived in the population between times 0 and } T}$ 

Usually,

Crude Death Rate = 
$$\frac{Number\ of\ deaths\ in\ a\ year}{Mid-year\ population}\cdot 1000$$

$$CDR = \frac{D}{\overline{P}}\cdot 1000$$
with  $\overline{P} = \frac{(P_1 + P_0)}{2}$ 

- >> Crude rate as no reference to smaller groups which might better represent the population likely to experience the event
- >> Influence of age structure



Source: Preston et al. (2001: 22)

N/A	BAVE									
	Swee	den, fema	les, 1992			Kazakh	stan, fem	ales, 1992		Statistics Division
Age	Mid-year	Deaths	Death	Proportion	Age	Mid-year	Deaths	Death	Proportion	!
group	population	during	rate	in age	group	population	during	rate	in age	
i		year		category	i		year		category	
	$N_i^{\mathrm{Sw}}$	$D_i^{\mathrm{Sw}}$	$M_i^{Sw}$	$C_i^{\mathrm{Sw}}$		$N_i^{\mathbf{K}}$	$D_i^{\mathbf{K}}$	$M_i^{K}$	$C_i^{\mathbf{K}}$	
0	59,727	279	0.00467	0.0136	0	174,078	3,720	0.02137	0.0200	
1-4	229,775	42	0.00018	0.0524	1-4	754,758	1,220	0.00162	0.0868	
5-9	245,172	31	0.00013	0.0559	5-9	879,129	396	0.00045	0.1011	
10-14	240,110	33	0.00014	0.0548	10-14	808,510	298	0.00037	0.0929	
15-19	264,957	61	0.00023	0.0604	15-19	720,161	561	0.00078	0.0828	
20-4	287,176	87	0.00030	0.0655	20-4	622,988	673	0.00108	0.0716	
25-9	311,111	98	0.00032	0.0709	25-9	733,057	752	0.00103	0.0843	
30-4	280,991	140	0.00050	0.0641	30-4	732,312	965	0.00132	0.0842	
35-9	286,899	197	0.00069	0.0654	35-9	612,825	1,113	0.00182	0.0704	
40-4	308,238	362	0.00117	0.0703	40-4	487,996	1,405	0.00288	0.0561	
45-9	320,172	643	0.00201	0.0730	45-9	284,799	1,226	0.00430	0.0327	
50-4	242,230	738	0.00305	0.0552	50-4	503,608	2,878	0.00571	0.0579	
55-9	210,785	972	0.00461	0.0481	55-9	301,879	3,266	0.01082	0.0347	
60-4	216,058	1,640	0.00759	0.0493	60-4	374,317	5,212	0.01392	0.0430	
65-9	224,479	2,752	0.01226	0.0512	65-9	256,247	6,866	0.02679	0.0295	
70-4	222,578	4,509	0.02026	0.0508	70-4	154,623	6,182	0.03998	0.0178	
75-9	184,102	6,745	0.03664	0.0420	75-9	149,917	8,199	0.05469	0.0172	
80-4	140,667	9,587	0.06815	0.0321	80-4	88,716	9,013	0.10159	0.0102	
85+	110,242	17,340	0.15729	0.0251	85 +	58,940	10,627	0.18030	0.0068	
All	4,385,469	46,256	0.01055	1.0000	All	8,698,860	64,572	0.00742	1.0000	
CDR		10.55	p. 1,000		CDR		7.42 p	. 1,000		



#### Age-specific death rate (ASDR)

Age specific death rate = 
$$\frac{Number\ of\ deaths\ in\ a\ year\ at\ age\ x}{Mid-year\ population\ at\ age\ x}\cdot 1000$$

$$_{n}M_{x}=\frac{_{n}D_{x}}{_{n}N_{x}}$$

- ASDR measures the incidence of death at each age
- ASDR may refer to single age or to grouped ages (e.g. 20-24, 25-29)
- Death rate is relatively high for infants under one year declines to its lowest levels for children and slowly increase thereafter



#### Infant Mortality Rate(IMR)

 One of the best-known and widely used available measure of mortality in early life

Infant mortally rate = 
$$\frac{Deaths \ under \ age \ 1 \ during \ year \ t}{Total \ live \ births \ in \ year \ t} \cdot 1000$$

- Denominator is live births (not than the mid-year population as in ASDR)
- Majority of infant deaths occurs in the first days and weeks or life
  - >> Deaths not evenly distributed over the first 12 months, mid-year population is not a valid indicator of average size of the population at risk of infant mortality



#### Under-Five Morality Rate (or 'Child Mortality')

- Widely used to measure, assess and monitor the progress of countries
  - >> MDG-4: Reduce child mortality, Target 4.A: Reduce by two thirds, between 1990 and 2015, the under-five mortality rate
  - >> IGME (Interagency group for child mortality estimation) estimates available at <a href="https://www.childmortality.org">www.childmortality.org</a>
- Not a real rate

#### **Definition**

Under-five mortality rate is the *probability* per 1,000 that a newborn baby will die before reaching age five, if subject to age-specific mortality rates of the specified year



#### Life tables

- Contain several functions that represent the effects of mortality on a population
  - Life expectancy, age-specific mortality rates, probability of dying by age x
- Cohort life tables trace the experience of a single birth cohort (e.g. all those born in 1950)
  - Have to wait for entire cohort to die to have full data
- Period life tables use a synthetic cohort to represent prevailing mortality conditions at present time
  - As if a cohort lived whole life under current mortality conditions



#### The period life table – Example (Preston et al. 2001)

Age x	$_{n}N_{x}$	$_{n}D_{x}$	$_{R}m_{X}$	$_{H}a_{\mathcal{X}}$	nQx	$\pi P_X$	$l_x$	$_{n}d_{x}$	$_RL_R$	$T_A$	$e_x^n$
0	47,925	419	0.008743	0.068	0.008672	0.991328	100,000	867	99,192	7,288,901	72.889
1	189,127	70	0.000370	1.626	0.001479	0.998521	99,133	147	396,183	7,189,709	72.526
5	234,793	36	0.000153	2.500	0.000766	0.999234	98,986	76	494,741	6,793,526	68.631
10	238,790	46	0.000193	3.143	0.000963	0.999037	98,910	95	494,375	6,298,785	63.682
15	254,996	249	0.000976	2.724	0.004872	0.995128	98,815	481	492,980	5,804,410	58.740
20	326,831	420	0.001285	2.520	0.006405	0.993595	98,334	630	490,106	5,311,431	54.014
25	355,086	403	0.001135	2.481	0.005659	0.994341	97,704	553	487,127	4,821,324	49.346
30	324,222	441	0.001360	2.601	0.006779	0.993221	97,151	659	484,175	4,334,198	44.613
35	269,963	508	0.001882	2.701	0.009368	0.990632	96,492	904	480,384	3,850,023	39.900
40	261,971	769	0.002935	2.663	0.014577	0.985423	95,588	1,393	474,686	3,369,639	35.252
45	238,011	1,154	0.004849	2,698	0.023975	0.976025	94,195	2,258	465,777	2,894,953	30.734
50	261,612	1,866	0.007133	2,676	0.035082	0.964918	91,937	3,225	452,188	2,429,176	26,422
55	181,385	2,043	0.011263	2.645	0.054861	0.945139	88,711	4,867	432,096	1,976,988	22,286
60	187,962	3,496	0.018600	2,624	0.089062	0.910938	83,845	7,467	401,480	1,544,893	18,426
65	153,832	4,366	0.028382	2.619	0.132925	0.867075	76,377	10,152	357,713	1,143,412	14.971
70	105,169	4,337	0.041238	2.593	0.187573	0.812427	66,225	12,422	301,224	785,699	11.864
75	73,694	5,279	0.071634	2.518	0.304102	0.695898	53,803	16,362	228,404	484,475	9.005
80	57,512	6,460	0.112324	2,423	0.435548	0.564452	37,441	16,307	145,182	256,070	6.839
85	32,248	6,146	0.190585	5.247	1.000000	0.0000000	21,134	21,134	110,889	110,889	5.247

Data source: United Nations, 1994.



#### Definition of the life table functions

Function	Definition
$l_x$	Number alive at exact age $x$ , out of the original number of births
$_{n}q_{x}$	Probability of dying between exact ages $x$ and $x+n$
$_{n}p_{x}$	Probability of surviving from exact age $x$ to exact age $x+n$
$_{n}d_{x}$	Number of deaths between ages $x$ and $x+n$
$_{n}L_{x}$	Average number alive in the interval between exact ages $x$ and $x+n$ . It also denotes the number of person-years lived in the interval between exact ages $x$ and $x+n$
$T_x$	Total population aged $x$ and over, or the total number of person- years lived from exact age $x$
$e_{_{\chi}}$	Expectation of life at exact age $x$ , i.e. the average number of years lived by a person from exact age $x$



#### Life table – Point and interval measures

Functions referring to exact age $x$	Functions referring to the interval between exact ages $x$ to $x+n$
$l_x$	$_{n}q_{x}$
$T_x$	$_{n}p_{x}$
$e_x$	$_{n}d_{x}$
	$_{n}L_{x}$

#### **Formatting conventions**

 $l_x$ ,  $d_x$ ,  $L_x$ , and  $L_x$  >> whole number of persons  $M_x$ ,  $d_x$ , and  $d_x$  >> five decimal places for rates and probabilities  $e_x$  >> two decimales places for life expectancy



- **1.** Age-specific death rate  $\binom{n}{n}M_x \rightarrow \binom{n}{n}M_x = \frac{\binom{n}{n}N_x}{\binom{n}{n}N_x}$
- 2. Probability of dying between ages x and x+n ( $_nq_x$ ) >> assuming that persons dying in the interval do so, on average, halfway through the interval

$$_{n}q_{x} = \frac{2n \cdot _{n}M_{x}}{2 + n \cdot _{n}M_{x}}$$

For open-ended age group  $\longrightarrow {}_{\infty}q_x = 1$ 

**3.** Probability of surviving from one age to the next  $\binom{n}{p_x}$ 

$$_{n}p_{x}=1-_{n}q_{x}$$



**4.** Number surviving at exact ages  $(l_x) \rightarrow l_{x+n} = l_x \cdot {}_n p_x$   $l_{x+n} = l_x - {}_n d_x$ 

>> At age 0, 
$$l_0$$
 = 100,000

5. Deaths between ages x and x+n  $\binom{n}{n}d_x = l_x \cdot {}_nq_x$   ${}_nd_x = l_x - l_{x+n}$ 



**6.** Average number alive between exact ages x and x+n ( $_nL_x$ )

$$\rightarrow {}_{n}L_{x} = \frac{n}{2} \cdot (l_{x} + l_{x+n})$$

For 
$$L_0$$
,  $\longrightarrow L_0 = 0.3l_0 + 0.7l_1$ 

For open-ended age group  $\longrightarrow {}_{\infty}L_x = \frac{l_x}{{}_{\infty}M_x}$ 

7. Total population aged x and over  $(T_x) \to T_x = \sum_{i=x} {}_{n}L_i$ 

For open-ended age group  $\longrightarrow T_x = {}_{\infty}L_x$ 

Working from the bottom of the life table  $\longrightarrow T_x = T_{x+n} + {}_nL_x$ 

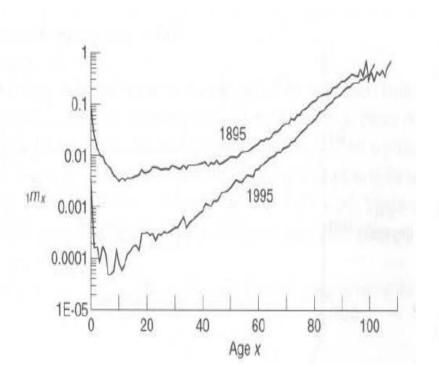


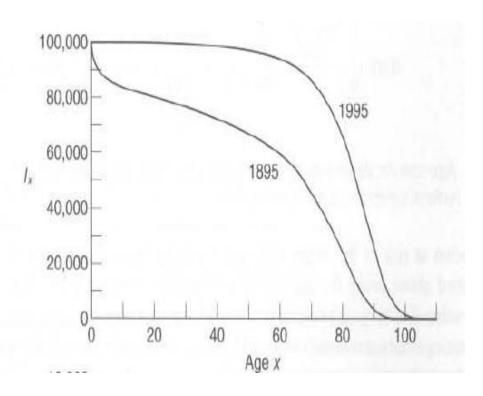
7. Expectation of life from age  $x(e_x) \rightarrow e_x = \frac{T_x}{l_x}$ 

$$\rightarrow$$
 Life expectancy at birth  $(e_0) = \frac{T_0}{l_0}$ 



#### Data checks: does the life table make sense?

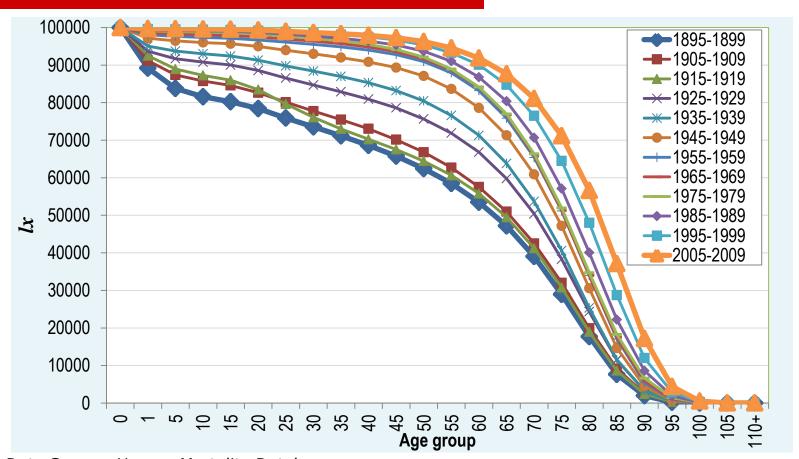




Source: Swedish females, 1895 vs 1995, Demography, Preston et. al. 2001



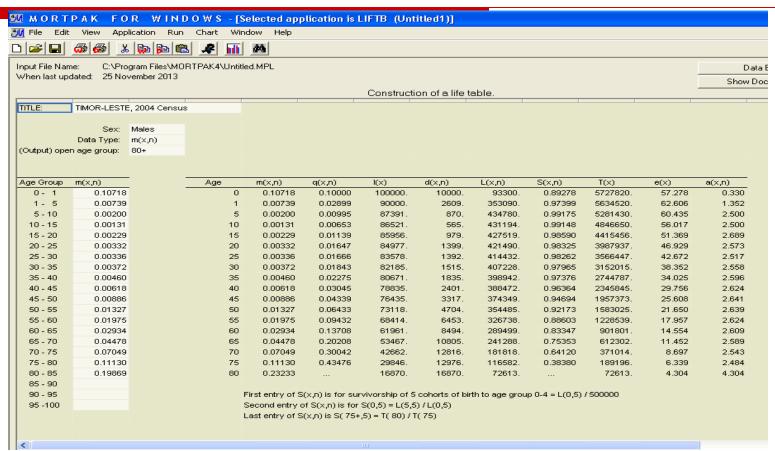
#### Rectangularization of the life table, Sweden, Females



Data Source: Human Mortality Database



## Example – using MortPak LIFTB Timor Leste, 2004 Census, Men



Data Source: NSD & UNFPA (2008), Mortality Monograph according to the 2004 census



#### Model life tables

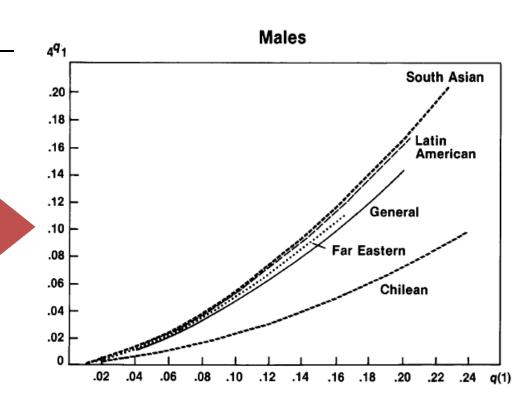
- Represent expected age patterns of mortality
- Created to estimate demographic parameters for countries with limited data
- Built on empirical studies of age-specific mortality patterns in the past
- Two groups of model life tables:
  - Coale-Demeny (1968, 1983): based on European populations
    - North, South, East and West European models
    - West only model based on some non-European life tables
  - United Nations (1982): based on developing countries
    - Latin American, Chilean, South Asian, Far Eastern, General



#### Model life tables (2)

Age-specific shape of mortality – relative probabilities of dying at different ages

Relationship between infant mortality  $({}_{1}q_{0})$  and child mortality  $({}_{4}q_{1})$ 



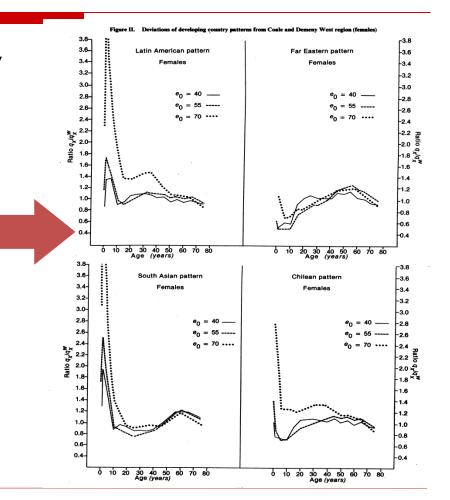
Source: United Nations (1990)



#### Model life tables (3)

Age-specific shape of mortality
– relative probabilities of
dying at different ages

Deviation of UN Model Life Tables from Coale-Demeny Model West, Females



Source: United Nations (1982)

T(X)



#### Model life tables (4)

#### United Nations Model Life Tables — Males

I(X)

Q(X)

M(X)

#### Latin American Pattern

A(X)

Level of mortality – each model has several different levels that correspond with a different life expectancies at birth  $(e_0)$ 

0	.23669	.20429	100000	20429	86313	3500000	35.000	0.330
1	.04672	.16631	79571	13234	283241	3413687	42.901	1.352
5	.00982	.04790	66337	3178	323742	3130446	47.190	2,500
10	.00511	.02522	63160	1593	311817	2806704	44.438	2.500
15	.00697	.03427	61567	2110	302841	2494887	40.523	2.633
20	.01036	.05051	59457	3003	290037	2192046	36.868	2.586
25	.01169	.05679	56454	3206	274346	1902009	33.691	2.528
30	.01332	.06449	53248	3434	257753	1627663	30.567	2.528
35	.01528	.07363	49814	3668	239996	1369910	27.500	2.526
40	.01757	.08418	46146	3885	221132	1129914	24.485	2.529
45	.02092	.09948	42262	4204	200930	908782	21.504	2.531
50	.02517	.11849	38058	4509	179185	707852	18.599	2.538
55	.03225	.14939	33548	5012	155420	528667	15.758	2.542
60	.04241	.19205	28537	5480	129217	373247	13.080	2.543
65	.06056	.26327	23056	6070	100230	244030	10.584	2.520
70	.08574	.35208	16986	5980	69747	143800	8.466	
75	.11840	.45210	11006	4976	42023	74053	6.729	2.461 2.386
			6030	3400	20953	32030		
80	.16226	.56382					5.312	2.295
85	.23745	*****	2630	2630	11077	11077	4.211	4.211
AGE	M(X)	Q(X)	I(X)	D(X)	L(X)	T(X)	E(X)	A(X)
0	.22881	.19840	100000	19840	86707	3599999	36.000	0.330
0	.22881 .04434	.19840 .15871	100000 80160	19840 12723	86707 286952	3599999 3513291	36.000 43.828	0.330 1.352
0 1 5	.22881 .04434 .00933	.19840 .15871 .04560	100000 80160 67438	19840 12723 3075	86707 286952 329502	3599999 3513291 3226339	36.000 43.828 47.842	0.330 1.352 2.500
0 1 5	.22881 .04434 .00933 .00487	.19840 .15871 .04560 .02408	100000 80160 67438 64363	19840 12723 3075 1550	86707 286952 329502 317940	3599999 3513291 3226339 2896838	36.000 43.828 47.842 45.008	0.330 1.352 2.500 2.500
0 1 5 10	.22881 .04434 .00933 .00487 .00667	.19840 .15871 .04560 .02408 .03281	100000 80160 67438 64363 62813	19840 12723 3075 1550 2061	86707 286952 329502 317940 309189	3599999 3513291 3226339 2896838 2578898	36.000 43.828 47.842 45.008 41.057	0.330 1.352 2.500 2.500 2.634
0 1 5 10 15 20	.22881 .04434 .00933 .00487 .00667	.19840 .15871 .04560 .02408 .03281 .04843	100000 80160 67438 64363 62813 60752	19840 12723 3075 1550 2061 2942	86707 286952 329502 317940 309189 296662	3599999 3513291 3226339 2896838 2578898 2269709	36.000 43.828 47.842 45.008 41.057 37.360	0.330 1.352 2.500 2.500 2.634 2.588
0 1 5 10 15 20 25	.22881 .04434 .00933 .00487 .00667 .00992 .01120	.19840 .15871 .04560 .02408 .03281 .04843	100000 80160 67438 64363 62813 60752 57810	19840 12723 3075 1550 2061 2942 3151	86707 286952 329502 317940 309189 296662 281263	3599999 3513291 3226339 2896838 2578898 2269709 1973048	36.000 43.828 47.842 45.008 41.057 37.360 34.130	0.330 1.352 2.500 2.500 2.634 2.588 2.529
0 1 5 10 15 20 25 30	.22881 .04434 .00933 .00487 .00667	.19840 .15871 .04560 .02408 .03281 .04843	100000 80160 67438 64363 62813 60752 57810 54658	19840 12723 3075 1550 2061 2942	86707 286952 329502 317940 309189 296662	3599999 3513291 3226339 2896838 2578898 2269709	36.000 43.828 47.842 45.008 41.057 37.360	0.330 1.352 2.500 2.500 2.634 2.588
0 1 5 10 15 20 25 30 35	.22881 .04434 .00933 .00487 .00667 .00992 .01120 .01277 .01470	.19840 .15871 .04560 .02408 .03281 .04843 .05451 .06192 .07093	100000 80160 67438 64363 62813 60752 57810 54658 51274	19840 12723 3075 1550 2061 2942 3151 3384 3637	86707 286952 329502 317940 309189 296662 281263 264933 247381	3599999 3513291 3226339 2896838 2578898 2269709 1973048	36.000 43.828 47.842 45.008 41.057 37.360 34.130	0.330 1.352 2.500 2.500 2.634 2.588 2.529
0 1 5 10 15 20 25 30 35 40	.22881 .04434 .00933 .00487 .00667 .00992 .01120 .01277 .01470 .01696	.19840 .15871 .04560 .02408 .03281 .04843 .05451 .06192 .07093	100000 80160 67438 64363 62813 60752 57810 54658 51274 47637	19840 12723 3075 1550 2061 2942 3151 3384 3637 3878	86707 286952 329502 317940 309189 296662 281263 264933 247381 228615	3599999 3513291 3226339 2896838 2578898 2269709 1973048 1691784 1426852 1179470	36.000 43.828 47.842 45.008 41.057 37.360 34.130 30.952 27.828 24.759	0.330 1.352 2.500 2.500 2.634 2.588 2.529 2.530 2.528 2.532
0 1 5 10 15 20 25 30 35	.22881 .04434 .00933 .00487 .00667 .00992 .01120 .01277 .01470	.19840 .15871 .04560 .02408 .03281 .04843 .05451 .06192 .07093	100000 80160 67438 64363 62813 60752 57810 54658 51274	19840 12723 3075 1550 2061 2942 3151 3384 3637	86707 286952 329502 317940 309189 296662 281263 264933 247381	3599999 3513291 3226339 2896838 2578898 2269709 1973048 1691784 1426852	36.000 43.828 47.842 45.008 41.057 37.360 34.130 30.952 27.828	0.330 1.352 2.500 2.500 2.634 2.588 2.529 2.530 2.528
0 1 5 10 15 20 25 30 35 40 45 50	.22881 .04434 .00933 .00487 .00667 .00992 .01120 .01277 .01470 .01696	.19840 .15871 .04560 .02408 .03281 .04843 .05451 .06192 .07093	100000 80160 67438 64363 62813 60752 57810 54658 51274 47637	19840 12723 3075 1550 2061 2942 3151 3384 3637 3878	86707 286952 329502 317940 309189 296662 281263 264933 247381 228615	3599999 3513291 3226339 2896838 2578898 2269709 1973048 1691784 1426852 1179470	36.000 43.828 47.842 45.008 41.057 37.360 34.130 30.952 27.828 24.759	0.330 1.352 2.500 2.500 2.634 2.588 2.529 2.530 2.528 2.532
0 1 5 10 15 20 25 30 35 40 45	.22881 .04434 .00933 .00487 .00667 .00992 .01120 .01277 .01470 .01696	.19840 .15871 .04560 .02408 .03281 .04843 .05451 .06192 .07093 .08140	100000 80160 67438 64363 62813 60752 57810 54658 51274 47637 43759	19840 12723 3075 1550 2061 2942 3151 3384 3637 3878 4228	86707 286952 329502 317940 309189 296662 281263 264933 247381 228615 208371	3599999 3513291 3226339 2896838 2578898 2269709 1973048 1691784 1426852 1179470 950856	36.000 43.828 47.842 45.008 41.057 37.360 34.130 30.952 27.828 24.759 21.729	0.330 1.352 2.500 2.500 2.634 2.588 2.529 2.530 2.528 2.532 2.532
0 1 5 10 15 20 25 30 35 40 45 50	.22881 .04434 .00933 .00487 .00667 .00992 .01120 .011277 .01470 .01696 .02029	.19840 .15871 .04560 .02408 .03281 .04843 .05451 .06192 .07093 .08140 .09663 .11564	100000 80160 67438 64363 62813 60752 57810 54658 51274 47637 43759 39531	19840 12723 3075 1550 2061 2942 3151 3384 3637 3878 4228	86707 286952 329502 317940 309189 296662 281263 264933 247381 228615 208371 186413	3599999 3513291 3226339 2896838 2578898 2269709 1973048 1691784 1426852 1179470 950856 742484	36.000 43.828 47.842 45.008 41.057 37.360 34.130 30.952 27.828 24.759 21.729 18.782	0.330 1.352 2.500 2.500 2.634 2.588 2.529 2.530 2.528 2.532 2.535 2.545
0 1 5 10 15 20 25 30 35 40 45 50	.22881 .04434 .00933 .00487 .00667 .00992 .01120 .01277 .01470 .01696 .02029 .02452 .03156	.19840 .15871 .04560 .02408 .03281 .04843 .05451 .06192 .07093 .08140 .09663 .11564	100000 80160 67438 64363 62813 60752 57810 54658 51274 47637 43759 39531 34960	19840 12723 3075 1550 2061 2942 3151 3384 3637 3878 4228 4571 5119	86707 286952 329502 317940 309189 296662 281263 264933 247381 228615 208371 186413 162227 135367 105456	3599999 3513291 3226339 2896838 2578898 2269709 1973048 1691784 1426852 1179470 950856 742484 556071	36.000 43.828 47.842 45.008 41.057 37.360 34.130 30.952 27.828 24.759 21.729 18.782 15.906	0.330 1.352 2.500 2.500 2.634 2.588 2.529 2.530 2.528 2.532 2.532 2.535
0 1 5 10 15 20 25 30 35 40 45 50 55 60 65 70	.22881 .04434 .00933 .00487 .00667 .00992 .01120 .01277 .01470 .01696 .02029 .02259 .02452 .03156	.19840 .15871 .04560 .02408 .03281 .04843 .05451 .06192 .07093 .08140 .09663 .11564 .14644 .18889	100000 80160 67438 64363 62813 60752 57810 54658 51274 47637 43759 39531 34960 29840	19840 12723 3075 1550 2061 2942 3151 3384 3637 3878 4228 4571 5119	86707 286952 329502 317940 309189 296662 281263 264933 247381 228615 208371 186413 162227 135367	3599999 3513291 3226339 2896838 2578898 2269709 1973048 1691784 1426852 1179470 950856 742484 556071 393844	36,000 43,828 47,842 45,008 41,057 37,360 34,130 30,952 27,828 24,759 21,729 18,782 15,906 13,198	0.330 1.352 2.500 2.500 2.634 2.588 2.529 2.530 2.528 2.532 2.535 2.541 2.545
0 1 5 10 15 20 25 30 35 40 45 50 55 60	.22881 .04434 .00933 .00487 .00667 .00992 .01120 .01277 .01470 .01696 .02029 .02452 .03156 .04164	.19840 .15871 .04560 .02408 .03281 .04843 .05451 .06192 .07093 .08140 .09663 .11564 .14644 .18889 .25961	100000 80160 67438 64363 62813 60752 57810 54658 51274 47637 43759 39531 34960 29840 24204	19840 12723 3075 1550 2061 2942 3151 3384 3637 3878 4228 4571 5119 5637 6284	86707 286952 329502 317940 309189 296662 281263 264933 247381 228615 208371 186413 162227 135367 105456	3599999 3513291 3226339 2896838 2578898 269709 1973048 1691784 1426852 1179470 950856 742484 556071 393844 258477	36.000 43.828 47.842 45.008 41.057 37.360 34.130 30.952 27.828 24.759 21.729 18.782 15.906 13.198 10.679	0.330 1.352 2.500 2.500 2.634 2.588 2.529 2.530 2.528 2.532 2.535 2.541 2.545 2.546
0 1 5 10 15 20 25 30 35 40 45 50 55 60 65 70	.22881 .04434 .00933 .00487 .00667 .00992 .01120 .01277 .01470 .01696 .02029 .02452 .03156 .04164 .05958	.19840 .15871 .04560 .02408 .03281 .04843 .05451 .06192 .07093 .08140 .09663 .11564 .14644 .18889 .25961	100000 80160 67438 64363 62813 60752 57810 54658 51274 47637 43759 39531 34960 29840 24204 17920	19840 12723 3075 1550 2061 2942 3151 3384 3637 3878 4228 4571 5119 5637 6284 6237	86707 286952 327502 317940 309189 296662 281263 264933 247381 228615 208371 186413 162227 135367 105456 73786	3599999 3513291 3226339 2896838 2578898 269709 1973048 1691784 1426852 1179470 950856 742484 556071 393844 258477 153022	36.000 43.828 47.842 45.008 41.057 37.360 34.130 30.952 27.828 24.759 21.729 18.782 15.906 13.198 10.679 8.539	0.330 1.352 2.500 2.550 2.634 2.588 2.529 2.532 2.532 2.535 2.545 2.545 2.546 2.523
0 1 5 10 15 20 25 30 35 40 45 50 55 60 65 70	.22881 .04434 .00933 .00487 .00667 .00992 .01120 .01127 .01470 .01696 .02029 .02452 .03156 .04164 .05958 .08453	.19840 .15871 .04560 .02408 .03281 .04843 .05451 .06192 .07093 .08140 .09663 .11564 .14644 .18889 .25961 .34804	100000 80160 67438 64363 62813 60752 57810 54658 51274 47637 43759 39551 34960 29840 24204 17920 11683	19840 12723 3075 1550 2061 2942 3151 3384 3637 3878 4228 4571 5119 5637 6284 6237 5235	86707 286952 329502 317940 309189 296662 281263 264933 247381 228615 208371 186413 162227 135367 105456 73786 44753	3599999 3513291 3226339 2896838 2578898 2269709 1973048 1691784 1426852 1179470 950856 742484 556071 393844 258477 153022 79236	36.000 43.828 47.842 45.008 41.057 37.360 34.130 30.952 27.828 24.759 21.729 18.782 15.906 13.198 10.679 8.539 6.782	0.330 1.352 2.500 2.550 2.534 2.588 2.529 2.530 2.528 2.532 2.532 2.541 2.545 2.546 2.523 2.464 2.390

D(X)

L(X)

Source: United Nations (1982)



#### Survival of children ever born

Indirect estimation of child mortality



#### Mortality estimates from population censuses: Introduction

- A group of questions can be used to obtain mortality data in a census
- Two distinctions:
  - a) Level and trend of mortality vs age pattern of mortality
    - Survival of children ever born: level and trend of mortality
    - Household deaths: age pattern of mortality
  - b) Deaths of younger persons vs. deaths of adults
    - Younger persons: survival of children ever born
    - Adults: household deaths
- All approaches are to supplement death registration data, not to replace it



#### Quick review - children ever born data

- Have been used for the past 50 years to collect data on infant and child mortality
- For every woman the following information is collected:
  - a) the total number of female children she has had in her lifetime.
  - b) the total number of male children she has had in her lifetime.
  - c) the number of female children who are surviving
  - d) the number of male children who are surviving



#### Survival of children ever born

- Ever born Surviving = Children deceased
- Children deceased / Ever born = Proportion deceased
- Life table measures of infant, child and young adult mortality may be derived from the proportion of deceased
  - In combination with data on age of mother



#### Brass type estimates

- Provide *indirect estimation* of level and trend of mortality for about 20 years prior to a census or survey
- Data required:
  - Number of women by
    - 5 year age group or;
    - Duration of marriage (5 year groups)
  - Total number of children born alive to women in corresponding
     5-year groups
  - Total number of children still alive (or deceased) at time of census by corresponding 5-year groups



## Brass type estimates (2)

Age group of mother in years	Age group index	Proportion of children dead approximates
15-19	1	q(1)
20-24	2	q(2)
25-29	3	q(3)
30-34	4	q(5)
35-39	5	q(10)
40-44	6	q(15)
45-49	7	q(20)
50-54	8	q(25)
55-59	9	q(30)



#### Brass type estimation – data checks

Women in the age group should include all women, not only those who respond to CEB/CS questions

>>Important to check in contexts where inappropriate to ask unmarried women about childbearing

		BANGLADESH (	CENSUS 1974 RETROSPECTIV	E SURVEY OF FERTILITY A	NO MORTALITY	
GI	NGE ROUP OF OMEN	TOTAL HOMEN	TOTAL BIRTHS	CHILDREN AT HOME	CHILDREN AMAY	CHILDREN DEAD
1	)-14 5-19	259 104 2 019 436	6 677 1 160 919	4 866 921 227	24 327	1 811 215 365
Note small	-24 -29	2 521 318 2 573 496	4 901 382 9 085 852	3 820 649 6 927 908	83 349 219 989	997 384 1 937 955
number of	-34 -39 -44	2 003 082 1 766 100 1 473 382	9 910 256 10 384 001	7 126 473 6 974 267 5 472 460	522 587 919 566 1 276 846	2 261 196 2 490 168 2 415 023
women in 0-14	49 54 59	1 473 382 1 128 791 1 040 877	9 164 329 6 905 673 5 963 087	3 664 328 2 601 163	1 276 846 1 281 801 1 441 061	1 959 544 1 920 863
age group;	-59 -0+	601 625 1 631 217	3 257 428 8 136 608	1 206 148 2 102 978	913 559 2 800 615	i 137 721 3 233 015
unmarried were	s.	204	0	0	0	0
not included	AL	17 018 632	68 876 212	40 822 467	9 483 700	18 570 045

Source: United Nations (1990)



#### Brass type estimation – data checks (2)

- Experience has shown that it is possible to get high quality responses to summary birth histories in any data collection exercise, including censuses
  - If both CEB and CS are understated, some cancellation of errors will occur
  - > But in practice, reporting of CS is more likely to be complete than reporting of CEB >> calculated proportions of deceased children are likely to be too low
- Make sure trends in children ever born/surviving/ deceased are consistent
- Check for missing data and/or editing



### Brass type estimation – data checks (3)

Example: missing or implausible values of CEB and CS data

Table 5.1 Percentage of cases where no editing of children ever born and children surviving data was required, by population group and age group

			1 / / 1 1		0	1 00	7 I		
	African		Coloured		India	n/Asian	White		
Age	CEB	CS	CEB	CS	CEB	CS	CEB	CS	
12-14	65.2	34.5	53.5	27.2	61.4	19.7	46.2	22.6	
15-19	73.5	44.0	63.7	37.2	68.8	24.6	55.9	28.9	
20-24	82.5	62.5	78.5	59.5	79.1	40.9	72.0	115	
25-29	88.2	75.6	87.6	75.4	88.0	64 80.	3 per ce	ent	
30-34	90.9	81.2	91.2	82.0	92.2		ed to be		
35-39	91.9	83.2	92.6	84.5	93.5	82 edi	ted		
40-44	91.4	83.3	92.5	84.7	93.3	83.0	71.0	02.1	
45-49	89.9	82.3	91.3	83.7	91.9	82.6	90.4	82.2	

Source: Dorrington & Moultrie (2001).



**Turkey**, 2000

Brass type estimation – data checks (4)

Average CEB should be realistic given country TFR and typical ages at childbearing

Unless fertility or child mortality are increasing, average CD should increase with age group

			chilabearing			
Age group of		T / 1050	Average	<b>7</b> 1100	Average children	Proportion deceased
women	Total women	Total CEB	CEB	Total CS	deceased (CD)	(CEB-CS)/CEB
15 - 19	3518257	294628	0.08	281296	0.003789	0.045
20 - 24	3263432	2078364	0.64	1991445	0.026634	0.042
25 - 29	2918825	4522719	1.55	4312404	0.072055	0.047
30 - 34	2457285	5700038	2.32	5395143	0.124078	0.053
35 - 39	2400808	7036619	2.93	6563946	0.196881	0.067
40 - 44	1985225	6707033	3.38	6131544	0.289886	0.086
45 - 49	1658012	6394157	3.86	5722904	0.404854	0.105

Source: UN Demographic Yearbook

Unless fertility has been rising, average CEB should increase with age group



#### Brass type estimation – data checks (5)

- Check sex ratio at birth implied by the CEB data for different mother age groups if gender is disaggregated (from age and sex structure)
  - Is it plausible?
  - Can help to identify underreporting of female births
- Is proportion of children surviving/deceased plausible?
  - Compare with other sources on child mortality

# A rapid assessment of CEB/CS data: Timor-Leste, 2004 census (1)

Age group	Total women	CEB	CS	CS/CEB
15 - 19	46,768	5,290	4,504	0.851
20 - 24	37,782	39,624	35,565	0.898
25 - 29	28,609	73,323	64,595	0.881
30 - 34	30,057	115,856	99,662	0.860
35 - 39	23,811	116,718	96,678	0.828
40 - 44	23,366	126,257	98,795	0.782
45 - 49	17,357	91,961	67,192	0.731



# A rapid assessment of CEB/CS data: Timor-Leste 2004 census (2)

- □ Proportion deceased for the 30-34 age group =(1-0.860)=0.140
  - Proportion of children deceased born to mothers of 30-34 years of age approximates q(5), the proportion of children born who die before their 5<sup>th</sup> birthday, about 7 years before data collection
- Compare with other estimates, e.g., UN Population Division estimates of under-5 mortality
  - 2004 census 'quick' estimates of q(5) = 140 per 1000 for 1997
  - UN Pop Division=120 per 1000 (for 1995-2000 period)
  - IGME = 123.6 per 1000 (for 1997.5)
  - Possible overestimation of q(5) in census data?



#### **UN Population Division: World Population Prospects**

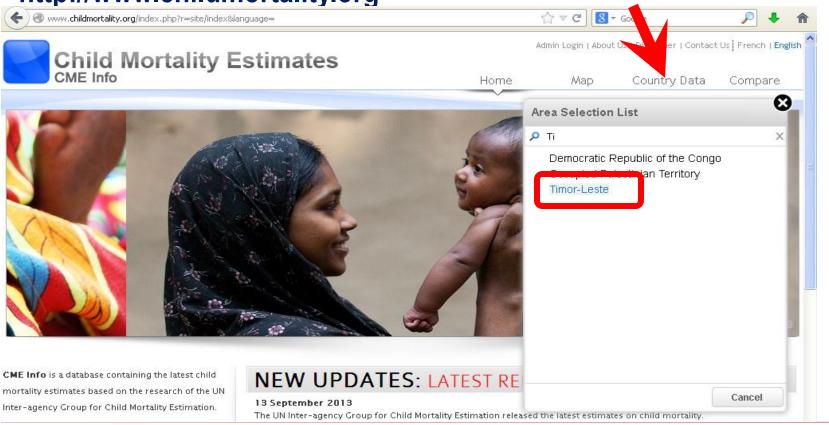
#### http://esa.un.org/wpp/Excel-Data/mortality.htm





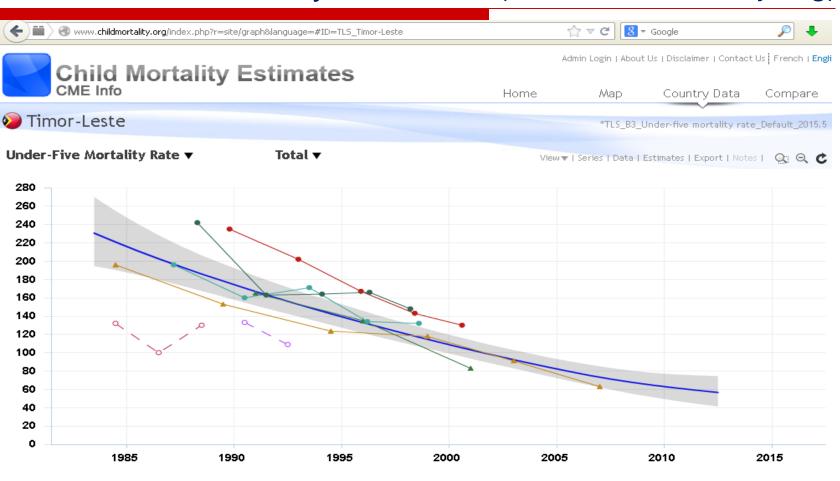
#### IGME: Child mortality estimates

http://www.childmortality.org





#### IGME: Child mortality estimates (www.childmortality.org)





#### Brass type estimation with MortPak QFIVE

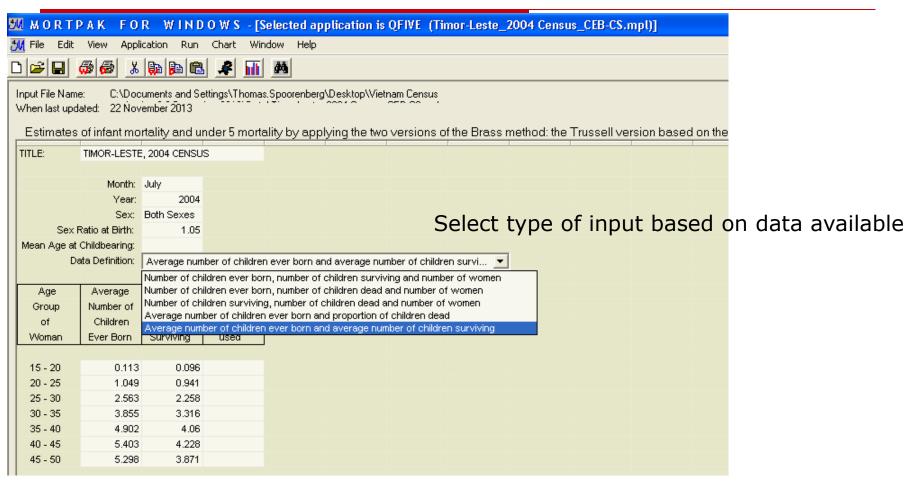
- Calculate the sex ratio at birth
  - If not available, can use standard 1.05
- Calculate the mean age of childbearing (only for UN model life tables)

$$M = \frac{17.5 \cdot B_{15-19} + 22.5 \cdot B_{20-24} + \dots + 47.5 \cdot B_{45-49}}{B_{15-19} + B_{20-24} + \dots + B_{45-49}}$$

where  $B_{x, x+n}$  = Births in past year to women age x to x+n

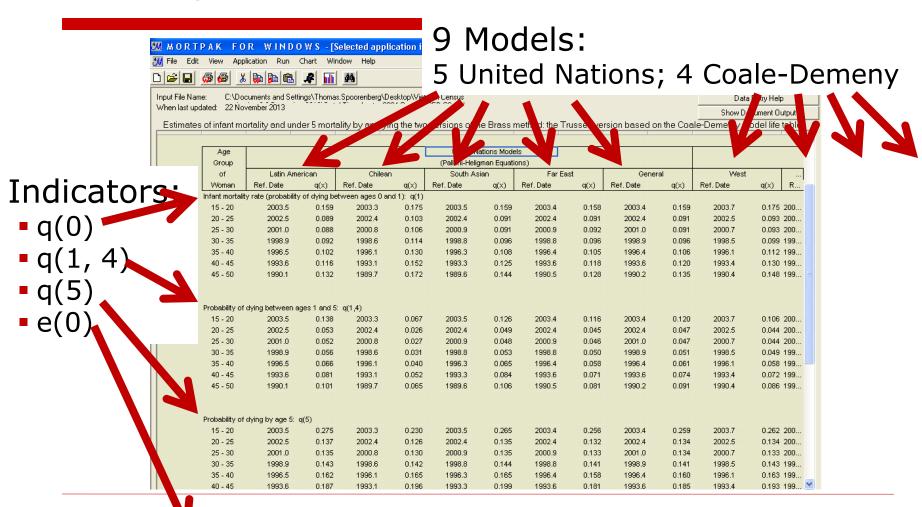


#### Brass type estimation with QFIVE





#### Brass output with QFIVE in MortPak

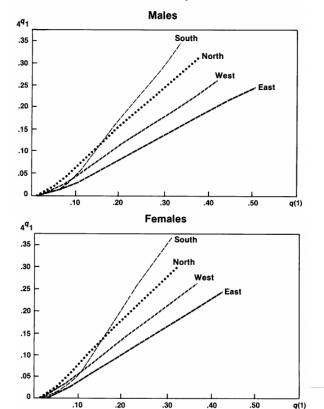




#### How to identify the right model life table (1)

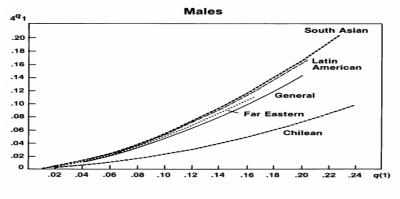
Relationship between mortality risk during the first year of life and between ages 1-4

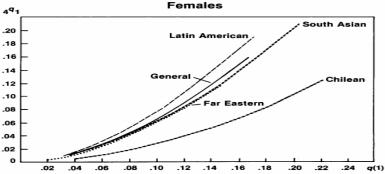
**Coale-Demeny Models** 



Source: United Nations (1990)

#### **United Nations Models**



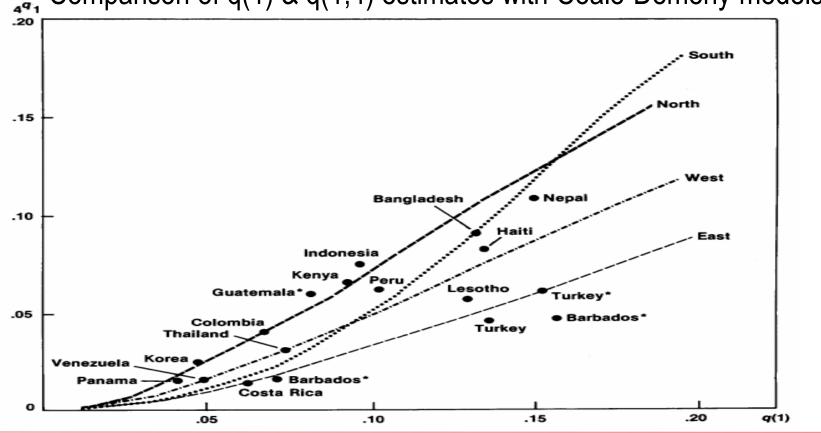




Source: United Nations (1990)

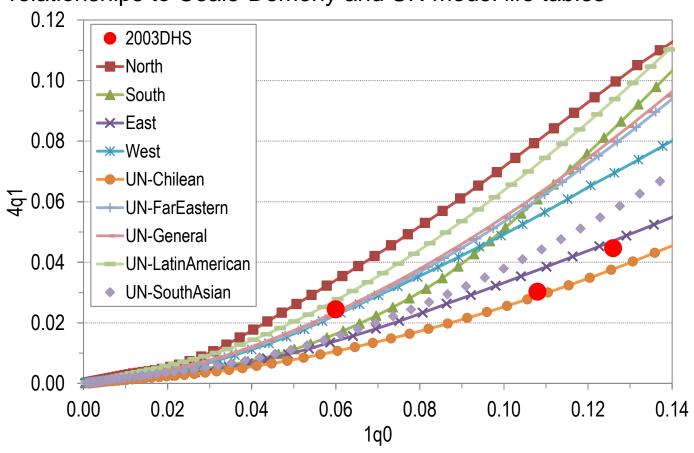
#### How to identify the right model life table (2)

Comparison of q(1) & q(1,4) estimates with Coale-Demeny models



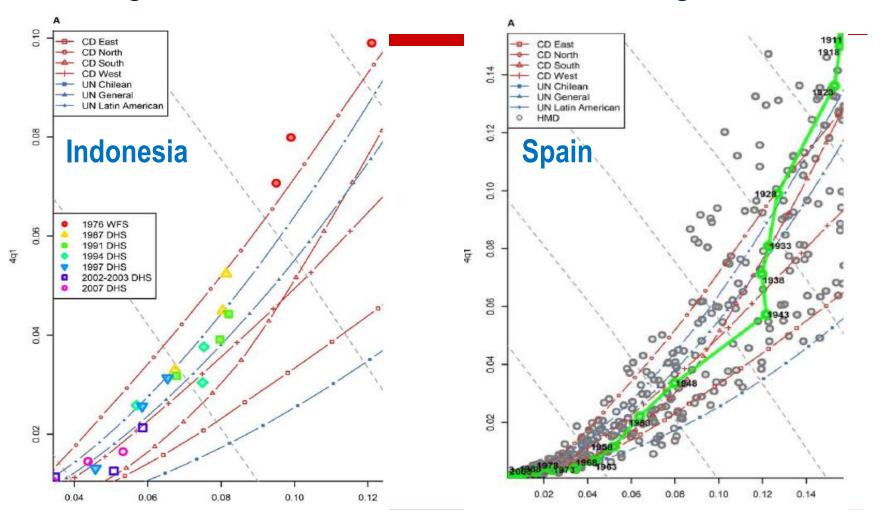
### How to identify the right model life table (3)

Direct estimates of q(0) and q(1,4) from Timor-Leste 2003 DHS, and the relationships to Coale-Demeny and UN model life tables





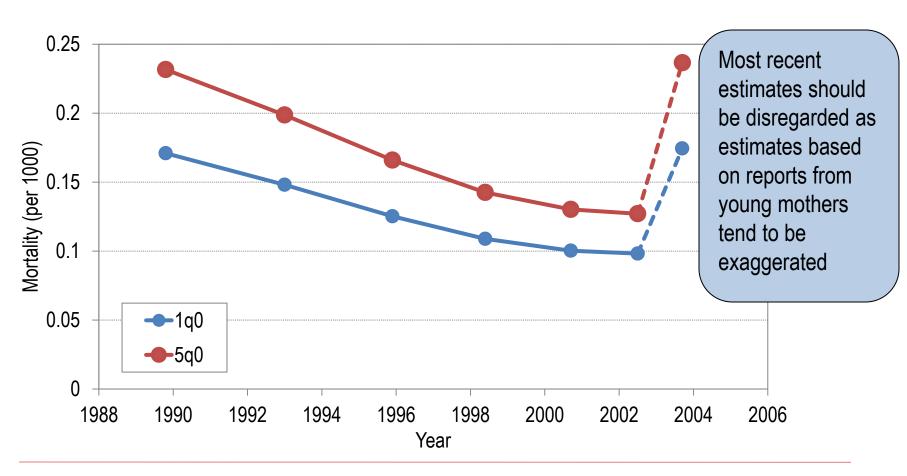
#### Change of families of Model Life Table through time



Source: Guillot et al. (2012)

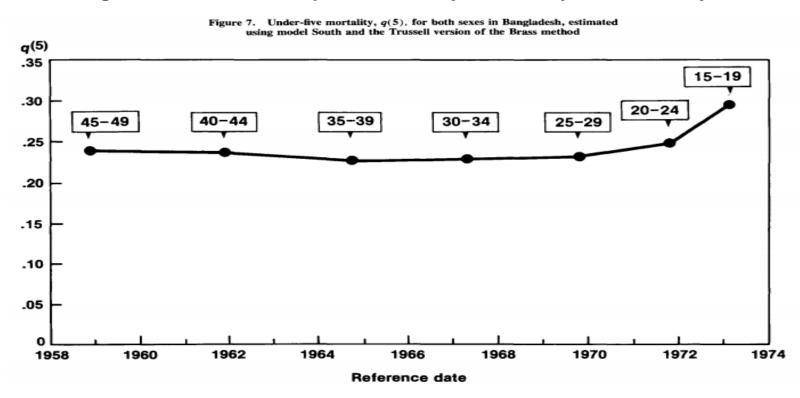


#### Estimated $_{1}q_{0}$ and $_{5}q_{0}$ over time, Timor-Leste, 2004 census



### Brass: relationship of mother's age and timing of the under-5 mortality estimates

#### Bangladesh, 1974 Retrospective Survey of Fertility and Mortality



Source: United Nations (1990)



#### Brass: Assumptions, violations (1)

- In any time period, mortality of children does not vary by five-year grouping of mothers
  - This assumption is usually violated for the mother age group 15-19, and to a lesser extent for the age group 20-24, because children of young mothers are known to have higher risk of mortality
  - Why?
    - First births have higher mortality risk than higher-order births and children of younger mothers are more likely to be first births
    - Youngest mothers tend to be socio-economically disadvantaged

Source: Moultrie et al. (2013)



#### Brass: Assumptions, violations (2)

- No correlation exists between mortality risks of children and survival of mothers in the population
  - This is a problem when certain mothers are not captured in the data (because of mortality or migration) whose children might also have higher mortality risk
  - Most common case is countries with high HIV prevalence results in downward bias in estimates
    - Younger mother age groups (20-24, 25-29) less likely to be biased
    - See for adjustment techniques: <a href="http://demographicestimation.iussp.org/content/effects-hiv-methods-child-mortality-estimation">http://demographicestimation.iussp.org/content/effects-hiv-methods-child-mortality-estimation</a>

Source: Moultrie et al. (2013)



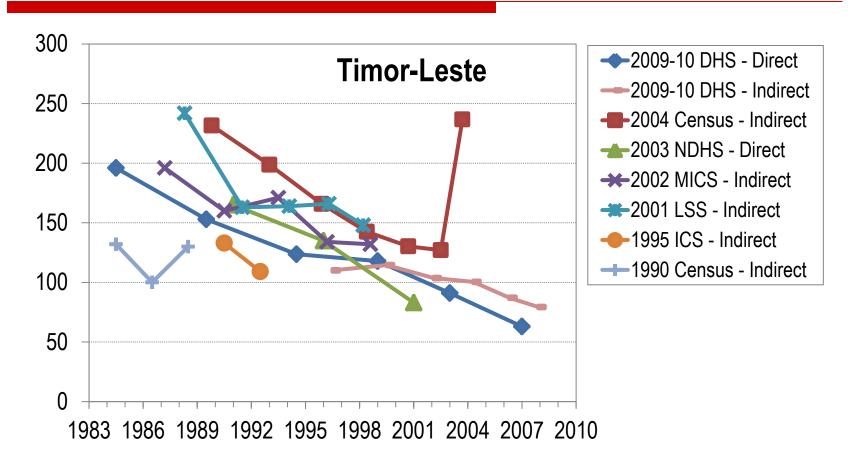
#### Brass: Assumptions, violations (3)

- Population age patterns of fertility and child mortality are adequately represented by the model patterns used in developing the method
- Any changes in child mortality in the recent past have been gradual and unidirectional
- Cross-sectional average numbers of children ever born by age adequately reflect cohort patterns of childbearing
- Note that when fertility has been changing (falling) rapidly, the Brass method will tend to over-estimate child mortality
- Variants of the technique grouping mothers by duration of marriage or time since first birth have been developed to address some of these issues

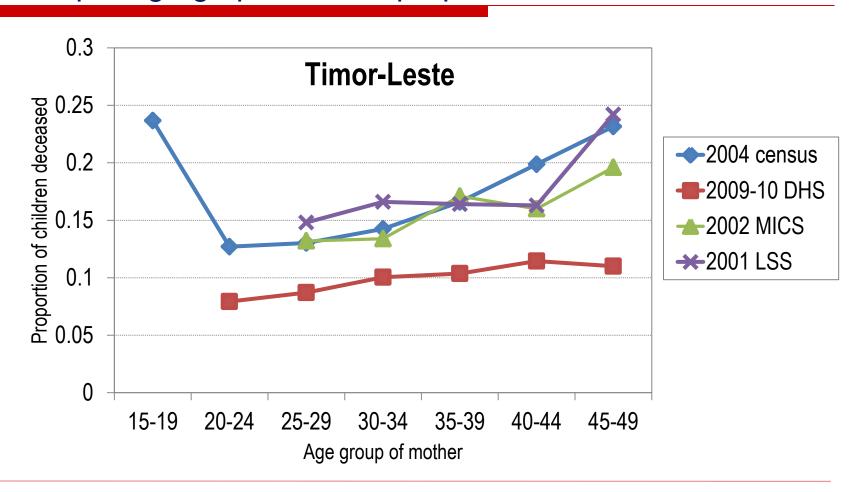
Source: Moultrie et al. (2013)



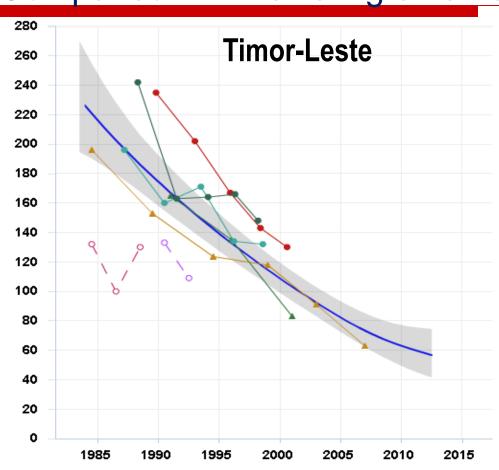
#### Quality of estimates: Checking multiple sources



#### Comparing age patterns of proportion of children deceased



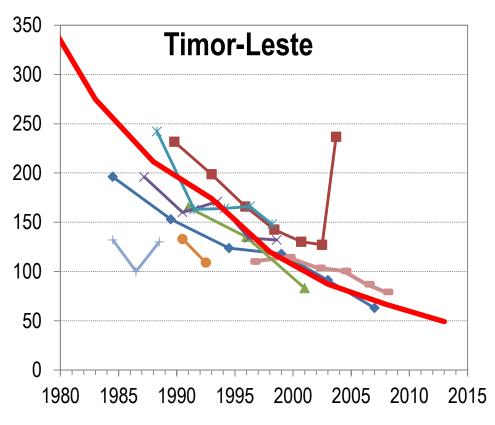
#### Comparison with existing external sources



#### **IGME** estimates

Source: www.childmortality.org

#### Comparison with existing external sources



UN Population Division (World Population Prospects)

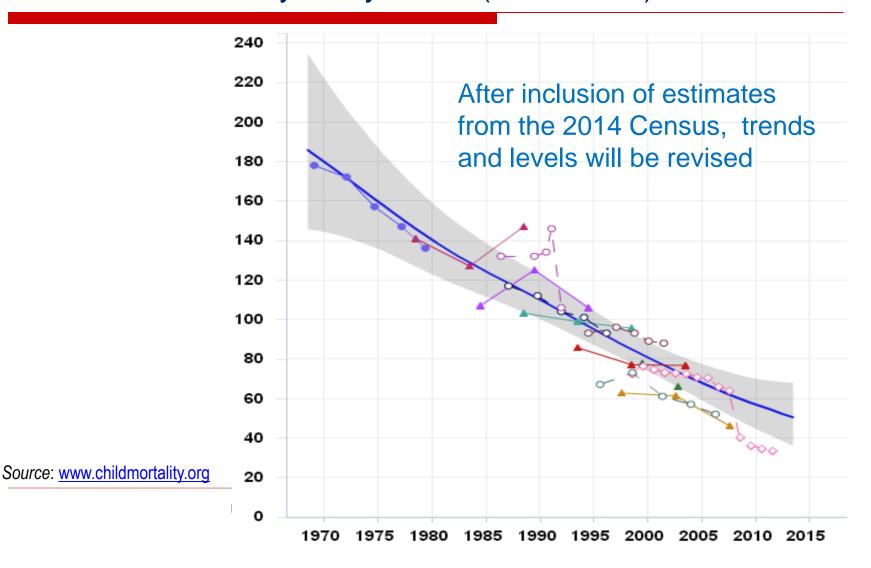
Source: http://esa.un.org/wpp/

#### Implied life expectancy at birth using Model Life Tables



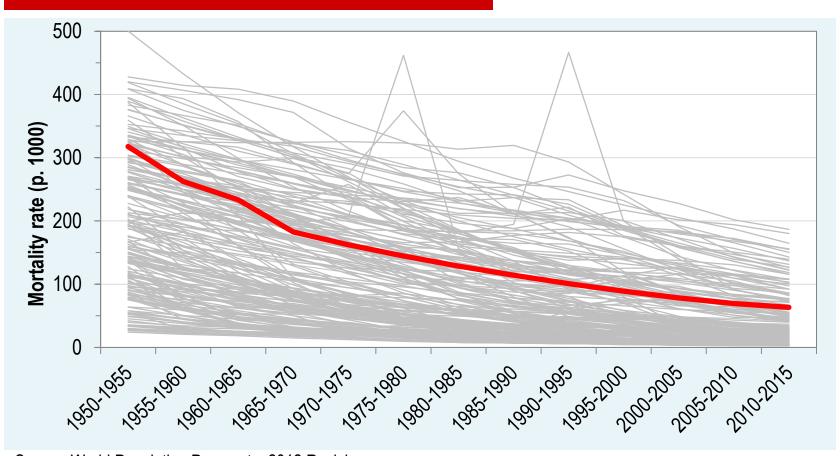


#### Under-five mortality in Myanmar (1968-2013)





#### Under-five mortality in Myanmar (1950-2015)



Source: World Population Prospects: 2012 Revision



#### References

- Feeney, G. (2009), *Rapid Assessment of Census Data on Children Born and Surviving*, available online at: <a href="http://demographer.com/2009-blog/rapid-assessment-of-ceb-and-cs-data/">http://demographer.com/2009-blog/rapid-assessment-of-ceb-and-cs-data/</a>
- Guillot, M., P. Gerland, F. Pelletier & A. Saabneh (2012), "Child mortality estimation: A global overview of infant and child mortality age patterns in light of new empirical data", *PLOS Medicine*, 9(8), e1001299
- Moultrie, T. et al. (2013), *Tools for Demographic Estimation*, Paris: IUSSP, available online at: <a href="http://demographicestimation.iussp.org/">http://demographicestimation.iussp.org/</a>
- United Nations (1982), *Model Life Tables for Developing Countries*, New York: United Nations, available online at: <a href="http://www.un.org/esa/population/publications/Model\_Life\_Tables/Model\_Life\_Tables.htm">http://www.un.org/esa/population/publications/Model\_Life\_Tables.htm</a>
- United Nations (1983), *Manual X: Indirect Techniques for Demographic Estimation*, New York: United Nations, available online at: <a href="http://www.un.org/esa/population/publications/Manual\_X/Manual\_X.htm">http://www.un.org/esa/population/publications/Manual\_X/Manual\_X.htm</a>
- United Nations (1990), *Step-by-step Guide to the Estimation of Child Mortality*, New York: United Nations, available online at:
  - http://www.un.org/esa/population/techcoop/DemEst/stepguide\_childmort/stepguide\_childmort.html
- United Nations Population Division (2012) *Updated UN Model Life Tables*, New York: United Nations, available online at: <a href="http://esa.un.org/unpd/wpp/Model-Life-Tables/download-page.html">http://esa.un.org/unpd/wpp/Model-Life-Tables/download-page.html</a>
- United Nations Population Division (2013) *World Population Prospects: The 2012 Revision*, New York: United Nations, available online at: <a href="http://esa.un.org/wpp/">http://esa.un.org/wpp/</a>



### Thank you

### ကျေးဇူးတင်ပါတယ်။

#### **Questions/comments?**

>> until 12 December:



>> After 12 December: spoorenberg@un.org